

Accuracy :-

close ness with which an instrument reading approaches the true value of the variable being measured.

Precision :-

Precision is a measure of the degree to which successive measurement ~~measure~~ (from) differ one another.

Sensitivity :-

The ratio of the magnitude of the output signal to the input signal.

Error :-

variation from the true value of the measured variable.

Resolution :-

The smallest changes in measured variable to which the instrument will respond.

Tolerance :-

It is the difference of the maximum measurement value to the actual value.

Measuring Instruments:-

These are of 2 types:-

(1) Absolute instrument

(2) Secondary instruments

→ Secondary instrument are of 2 types:-

(1) Digital

(ii) Analog

→ Again Analog instruments is of 3 type;

(i) Indicating (ii) Recording (iii) Integrating

→ The classification of Analog instruments are indicating type instruments, Recording type instruments and Integrating type instruments.

→ Indicating type instruments:-

These type of instruments indicate the instant value of the quantity to be measured.
eg → Ammeter, Voltmeter.

→ Recording type instrument

These type of instruments are indicating instruments with a recording arrangement.
eg → Recording instruments for frequency, Power factor.

Essentials of an indicating type instruments:-

An indicating is a moving instrument.

Deflecting Torque :-

The torque is necessary to move the pointer of the instrument from its zero position. Deflecting torque can be produced by utilising any one effect of the following;

- (i) Magnetic effect
- (ii) Electro dynamic effect
- (iii) Electro magnetic induction effect
- (iv) Electro static effect
- (v) Chemical effect
- (vi) Thermal effect.

Controlling Torque :-

Controlling is essential to balance or oppose the deflecting torque. Also this torque brings the pointer to '0' position after the measure quantity is withdrawn. This torque can be provided by 2 methods,

(1) Gravity control :-

which is provided by a small weight called controlled weight attached to the moving system. This torque produced due to the gravitational force acting on it.

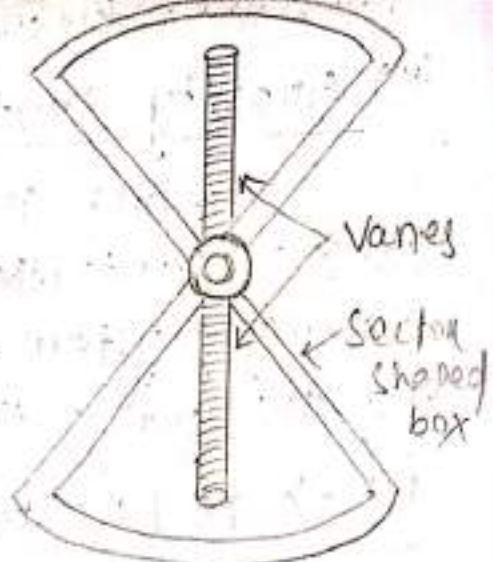
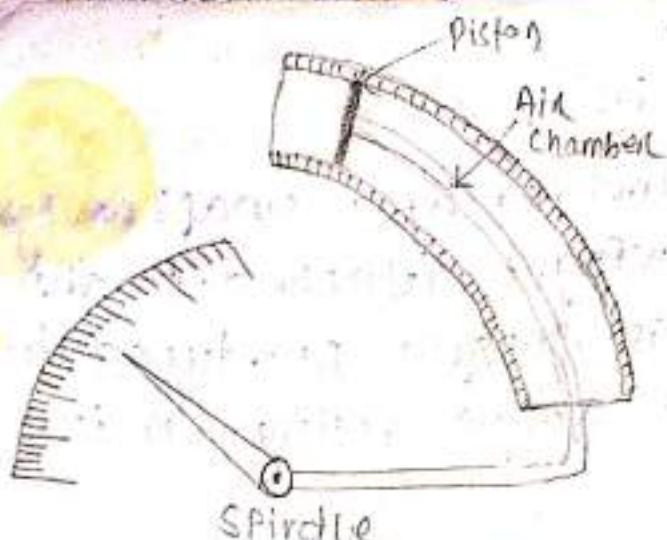
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Damping Torque :-

with the current is suddenly increased from zero to certain value and if there is no damping, the pointer will oscillate about its final position due to inertia of the moving system. when a damping device is used the pointer moves slowly and reaches its final position without oscillation.

(1) Air friction damping

(2) Eddy current damping

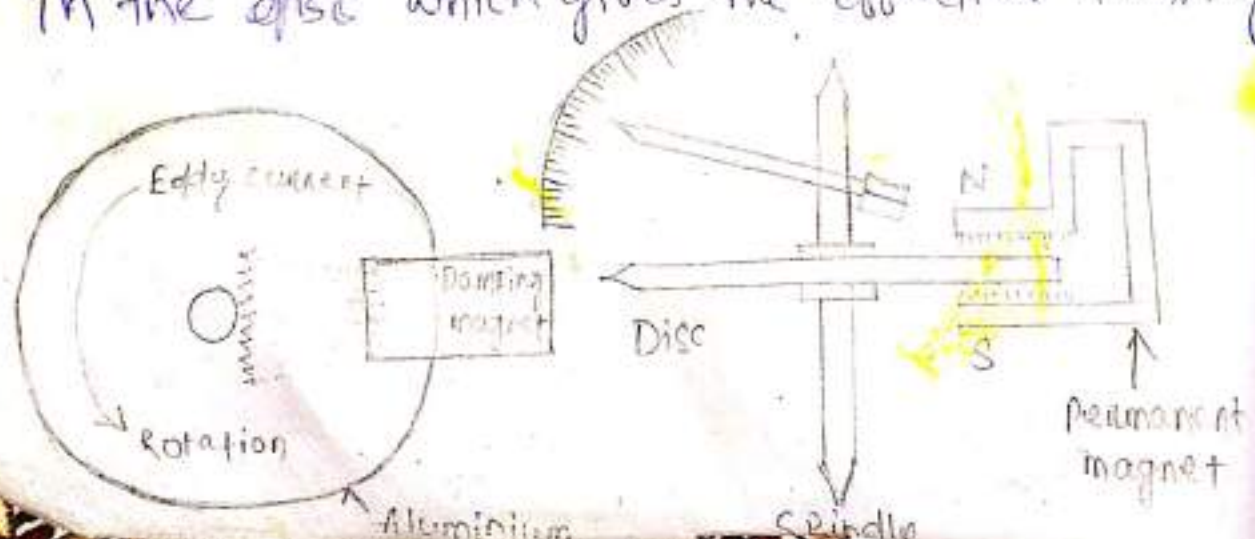


Air friction damping

The spindle to which the pointer is attached has vanes which moves in a sector or air chamber. As the pointer is deflected the vanes moves in the chamber against the air pressure. So the compressing of the air at the back provides the required damping.

Eddy current damping :-

In such damping a conducting but non magnetic material disc is fixed on the spindle when the pointer moves the disc also moves, so the flux is cut by the disc and the eddy current are induced in the disc which gives the effective damping.



CHAPTER: 2

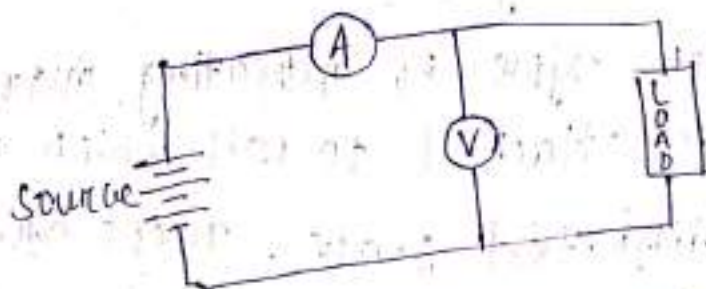
Voltmeter & Ammeter :-

Voltmeter :-

A voltmeter is used to measure the potential difference between the two points of circuit. It is connected in parallel with the circuit. The voltmeter is always design with very high internal resistance.

Ammeter :-

An ammeter is used to measure the flow of current in a circuit. So it is connected in series with the circuit. So, an ammeter is design with very low internal resistance.



The basic principle of voltmeter and ammeter is same. Both are current operated device. That is the deflecting torque is produced when current flows through their operating coils.

In ~~not~~ voltmeter the torque produced is directly proportional to the current flowing through the operating coils, which is proportional to the measured voltage.

* The types of indicating type instruments are:

- (1) M.C type used for DC ckt only.
(Moving coil)
- (2) MI type used for both AC and DC type ckt.
(Moving iron)
- (3) Hot wire type used for both AC and DC ckt.
- (4) Thermo couple type used for " " "
- (5) Electro static type " " "
- (6) Indicating type used for AC ckt only.

Moving coil (MC type) :-

- PMMC type
- Dynamometer type

In this type of indicating instrument the pointer is attached to coil which moves over the calibrated scale. These are of

- 2 type (i) → PMMC
(ii) → Dynamometer

PMMC :-

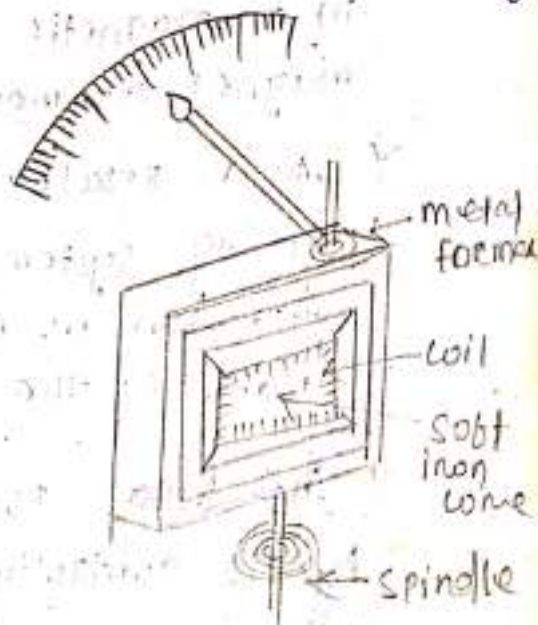
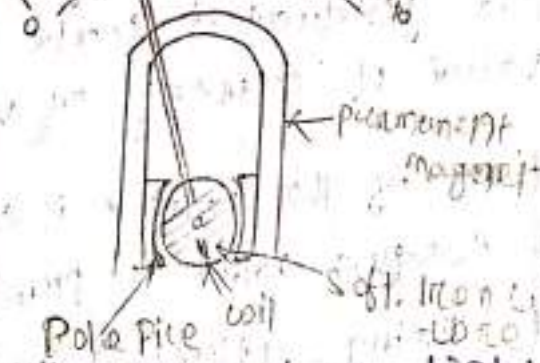
These instruments are either used as ammeters or voltmeters and suitable for dc work only.

Principle

→ This type of instrument is based on the principle that when a current carrying conductor is placed in a magnetic field a mechanical force act on the conductor.

→ The coil placed in the magnetic field and carrying the operating current is attached to the moving system. With the movement of the coil the pointer moves over the scale to indicate the electrical quantity being measured.

Construction



→ It consist of a light rectangular coil of many turns of thin wire wound on an aluminium former, inside which is an iron core.

→ The coil is pivoted upon jewel bearing and is mounted between the cores of a permanent magnet.

→ The current is lead into and out of the coil by two control, here bring one about the other below the coil.

The springs also provides the controlling torque. The damping torque is provided by eddy current induced in the aluminium former as the coil moves from 1 coil to another.

Working :-

When the instrument is connected in the circuit to measure the current or voltage the operating current flows through the coil.

Since the coil is carrying and is placed in a magnetic field of the permanent magnet as mechanical force is action it.

As a result the pointer attached to the moving system moves in a clock wise direction over the graduated scale to indicate the value of current or voltage.

The final position of the pointer is controlled by the controlling torque which is produced by the two air spring attached to the spindle.

The aluminium former over which the coil is wound provides the necessary damping torque.

Torque eqn :-

Let $B =$ flux density Wb/m^2

$l =$ length

$I =$ current in amp

of 20 x sectional area
 N = no. of turns

Deflecting force
 $F_d = NI \sin \theta$

Deflecting torque
 $T_d = BINA$

Controlling torque
 $T_c = k\theta$

$k = \text{spring constant}$
 $\theta = \text{angle of deflection}$

At final position
 $T_d = T_c$

$$BINA = k\theta$$

$$\Rightarrow \theta = \frac{BINA}{k}$$

Advantages:

- They have non-uniform scale
- High torque / wt. ratio
- It is very accurate

Disadvantage:

- They can not be used in AC
- It is very costly

Uses:

It is used in voltmeter, ammeter and galvanometer.

Torque equation

$$T_d = NBI A$$

$$\therefore T_d = GI$$

where $GI = NBI A = \text{constant}$

The controlling torque is provided by the spring & is proportional to the angular deflection of the pointer. $T_c = k\theta$

where $T_c = \text{controlling torque}$

$k = \text{spring constant}$
 $\theta = \text{angular deflection}$

At the final steady state position $T_d = T_c$

$$\therefore GI = k\theta \text{ so, } \theta = GI/k$$

$$\text{or } I = (k/GI)\theta$$

Thus the deflection is directly proportional to the current passing through the coil. The pointer deflection can therefore be used to measure current.

Dynamometer type instrument

These instruments are the modified form of PMMC type instrument. Here the magnet field, is not produced by the permanent magnet. But by two air port fixed coil placed on either sides of the moving coil.

Such instrument can be used as ammeters or voltmeter but generally they are used as watt meter.

They are suitable for both ac and dc.

Principle

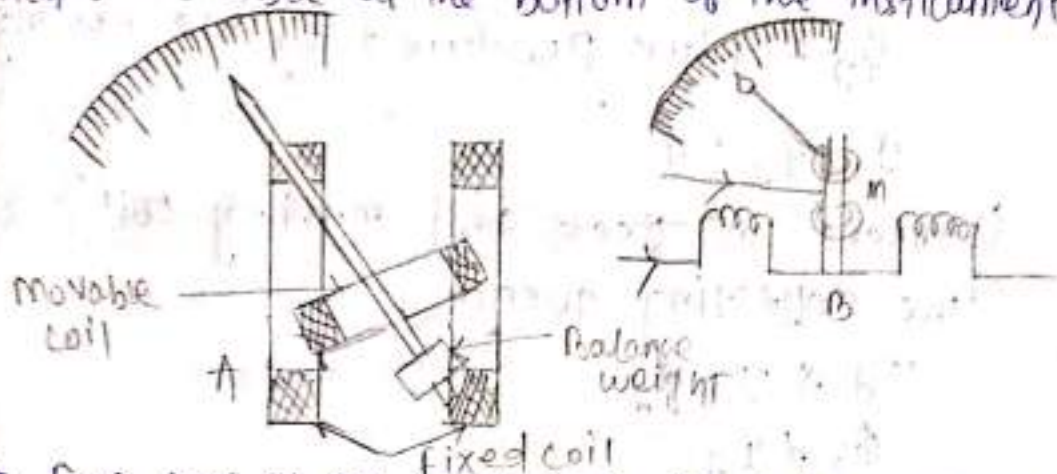
This instruments are based on the principle that mechanical force exist between the current carrying conductors.

Construction

It is essentially consist of a fixed coil and a moving coil. The fixed coil is divided into two equal part which are placed closed together and help to each other. The M.E is pivoted in between the 2 fixed coils and carries a pointer.

The current is lead into an out of the moving coil by means of a spiral hair spring which provides the controlling torque.

Air friction damping is provided by means of the aluminium vanes that move in the sector shape chamber at the bottom of the instrument.



- For use as an ammeter or voltmeter the fixed coil and moving coil are so connected that the same current flows through the 2 coils.
- Due to these current the mechanical force exist between the coil.
- The result is that the moving coil M moves the pointer over the scale.
- The pointer comes to rest at a position where the deflecting torque is equal to the controlling torque. Since the polarity of the fields produce by both fixed and moving coil is reversed by the reversal of current.
- The deflection of the moving system is always in the same direction.
- So for this reason dynamometer type instrument can be used for both ac and dc measurement.

Torque eqn. :-

Let ϕ_1 = Flux density of fixed coil

ϕ_2 = Flux produced by the moving coil

$$I_1 = I_2 = I$$

(Current in fixed and moving coil)

The deflecting torque

$$T_d \propto I_1 \phi_2$$

$$\phi_2 \propto I_2$$

$$T_d \propto I_1 I_2$$

$$T_d = k_1 I_1 I_2$$

$$T_c = k_2 \theta$$

$$T_d = T_c \Rightarrow k_1 I_1 I_2 = k_2 \theta$$

$$\boxed{\theta \propto I^2} \quad \text{Ammeter}$$

$$\boxed{\theta \propto V^2} \quad \text{Voltmeter}$$

Advantage :-

→ These instruments can be used for both ac and dc.

A PMMC instrument cannot be used as a wattmeter but dynamo-type instruments can be used as a wattmeter.

Disadvantage :-

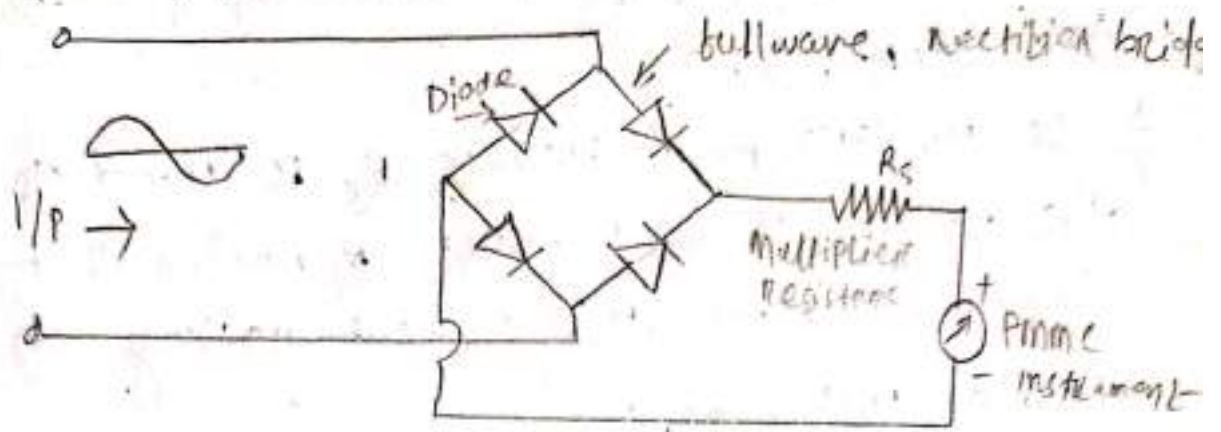
→ It is less sensitive

→ It is costly

Uses :-

Ammeter, voltmeter, wattmeter

Rectifier type instrument :-



- Rectifier type instrument are used for measurement of AC voltage and accurate by using a rectifier circuit, which convert AC to a unidirectional dc.
- And then using ammeter to dc to indicate the value of the rectified ac.
- The indicating instrument is PMMC instrument type.
- The arrangement which employ a full wave rectifier circuit using 4 diode.
- Rectifier instrument are particularly suited to measurement of communication circuit, and for all other light current work.
- where the voltages are low and resistance is high.
- It is essential that for this application that the current taken by the voltmeter does not exceed 1mA so that there are no loading effect and the rectifier

CHAPTER - 03

Watt meters :-

- (i) Dynamo meter type or moving coil type
- (ii) Induction type

(b) ~~Dynamo meter type~~ :-

→ A wattmeter as its name implies measures electrical power given to or developed by an electric apparatus or circuit a wattmeter may be of two type.

- (i) Dynamometric type
- (ii) Induction type

(i) Dynamometer type :-

→ It consist of two fixed coil C_1 and C_2 connected in series with load. they are known as current coils.

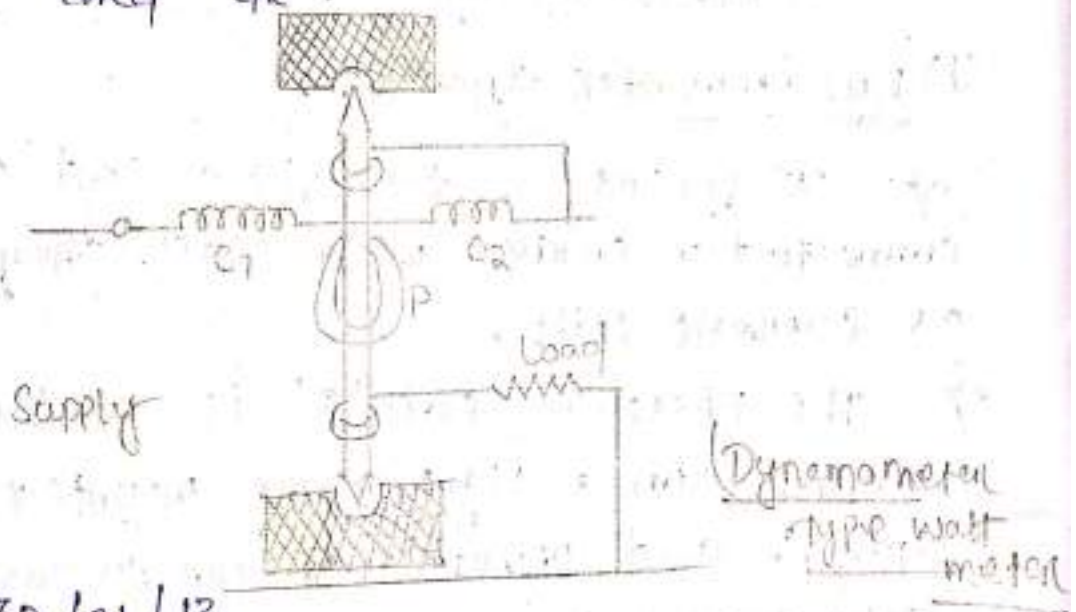
→ The pressure coil 'P' is of fine wire wound on a light frame mounted on a spindle and pivoted to turn to the magnetic field produced by the current coils.

→ The control torque for such instruments is provided by two spiral spring of Phosphoric bronze. These springs are also provides a path to load the current in an out of the pressure coil.

→ The pointer is attached to the spindle which moves over a graduated scale. To control the pressure coil current each at high

resistance is connected in series with the pressure coil.

- Under the action of the two fields due to the fix end moving coil, the moving coil moves round against the action of spiral spring.
- The torque depending on the product of current in two coils that is the torque is proportional to the power.
- The power as indicated by the scale is the mean power.
- These meters can be used on both ac and dc.



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Moving iron type instruments:-

These are of two types:-

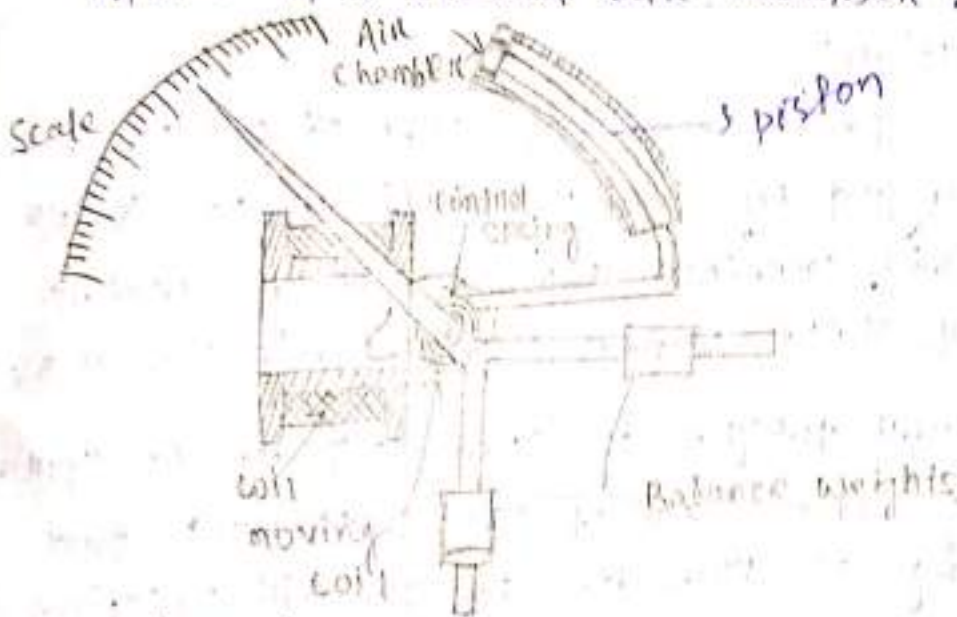
- (1) Attraction types
- (2) Repulsion types

This type of instruments are used for measurement of AC and DC voltage.

Attraction type :-

Construction :-

- It consists of a cylindrical coil which is kept fixed on overcoil shaped soft iron is attached to the spindle in such a way that it can move in or out of the coil.
- A pointer is attached to the spindle so that it is deflected with the motion of the soft iron.
- The controlling torque is provided by one spiral spring arranged at the top of the moving element.
- The damping torque is provided by the aluminium vane attached to the spindle which moves in a closed air chamber.



Working :-

- When the instrument is connected in the circuit to measure the voltage or current the operating current flowing through the coil and setup a magnetic field, or the coil behaves like a magnet.

has been
∴ So it attracts the soft iron piece towards it.

∴ The result is that the pointer attached to the moving system moves from '0' position.

∴ The pointer will come to rest at a position where deflecting torque is equal to the controlling coil.

∴ If the current in the coil is reversed the direction of the deflecting torque remains unchanged: so it is used for both ac and dc.

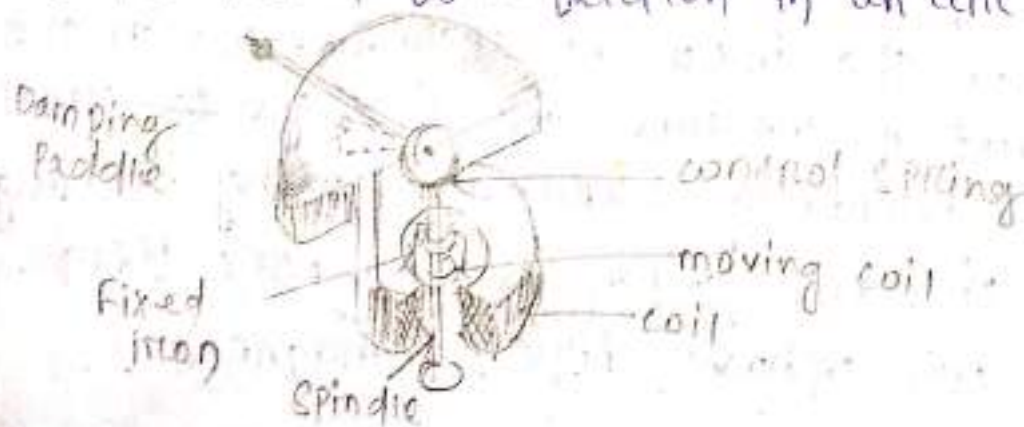
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Repulsion type :-

Construction :-

It consists of two soft iron pieces or vanes surrounded by a fixed cylindrical hollow coil which carries the operating current. One of these vanes is fixed other one is movable.

Control torque is provided by one spiral spring at the top of the instrument. And damping is provided by the air friction due to the motion of a vane in an air chamber.



Working:

- When current to be measured flows through the coil a magnetic field is setup by the coil.
- This magnetic field magnetises the two vanes in the same direction i.e. same polarity and developed at the same end of the vanes.
- Since the adjacent sides vanes are of same polarity and the two vanes repel each other.
- As the fixed vane can not move the movable vane deflects and causes the pointer to move from '0' position.
- The pointer will come to rest at a position where deflecting torque is equal to controlling torque. This is used for both ac and dc.

Torque eqn:

$$T_d \propto I^2$$

$$T_c = k \theta$$

$$T_d = T_c$$

$$I^2 = k \theta$$

$$\theta \propto I^2$$

where θ = angle of deflection,

Application:

The MI instruments are primarily used for ac measurement. They are be used for dc measurement but usually not done so as it's less accurate.

Advantages!—

- It is cheap
- It is used for both ac and dc

Disadvantages!—

- It is less accurate
- Less sensitive
- The scale is not linear.

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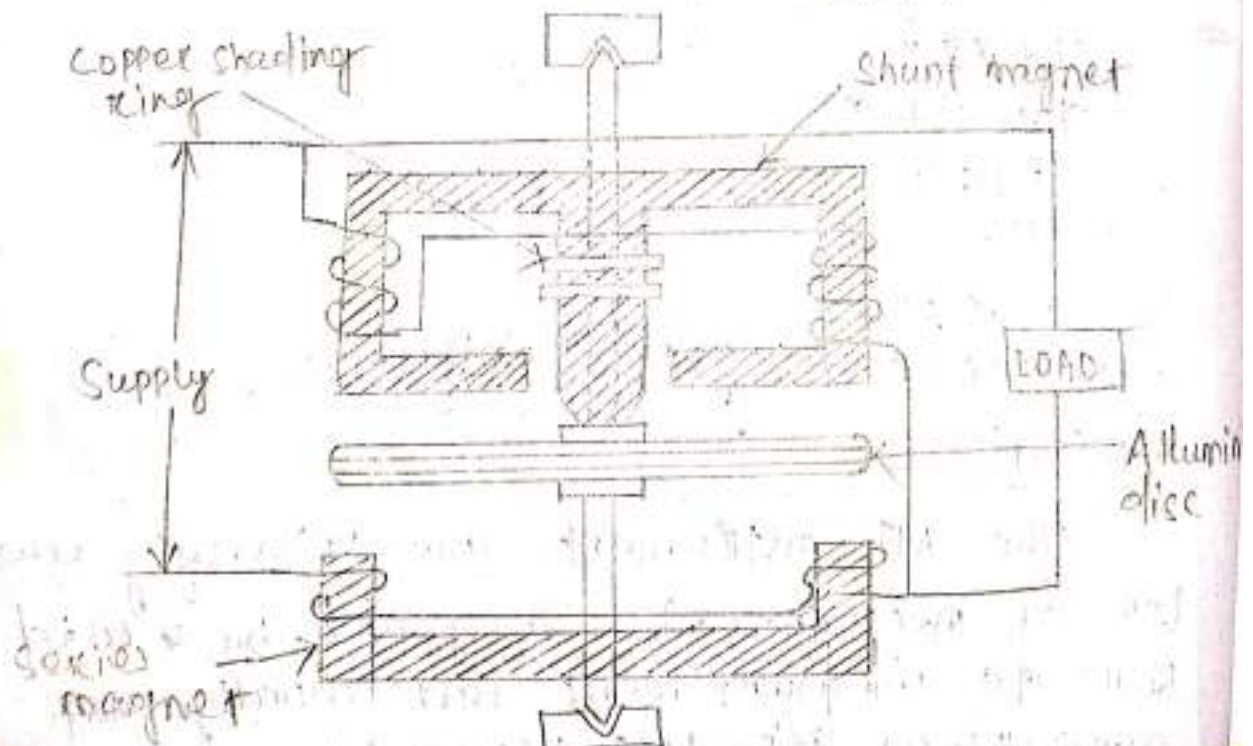
Induction type watt meter!—

Construction!—

This type of watt meter is used on ac only. Induction type wattmeter consist of 2 electro magnets.

(a) series magnet → It is connected in series with the load.

(b) shunt magnet → it is connected in parallel with the load.



A thin aluminium disc is mounted between the two magnets. When the current flows in the magnet the aluminium disc cuts the flux of both magnet so eddy currents are induced in the disc. The eddy currents and inducing fluxes interact and produce a deflecting torque.

→ A few Cu-rings are fixed on the central part of the shunt magnet to make the resultant flux in the shunt magnet leg behind the applied voltage by 90° .

→ current phase displacement between the shunt and series magnet fluxes can be obtained by adjusting the Cu-shading rings.

→ The instrument is provided with the spring and produces a controlling torque.

→ Eddy current damping used for this instrument.

Advantages:—

→ These instruments have larger deflecting torque.

→ They have a very long scale up to 300'.

Disadvantages:—

→ They have a ~~mea~~heavy moving system and are less accurate.

→ ~~Their~~ power They are power consumption is high.

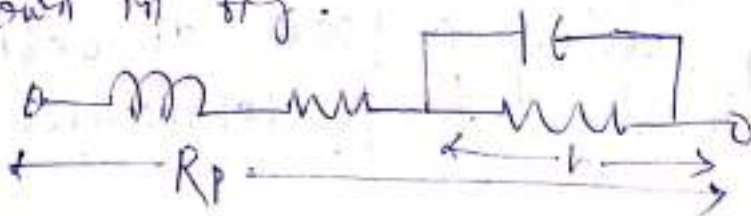
→ They are used only on AC.

Error in dynamometer type wattmeter!

The error in dynamometer type wattmeter are:-

- 1) Pressure coil inductance
- 2) Pressure coil capacitance
- 3) Error due to mutual inductance effects
- 4) Error caused due to wrong connections
- 5) Eddy current errors
- 6) Stray magnetic field errors
- 7) Error caused by vibration of moving system.
- 8) Temperature errors.

The method of connections are two error (i) a capacitor must be connected in parallel with a portion of multiplier as shown in fig.



The error (ii) can be corrected making inductive reactance equal to capacitive reactance i.e. ($X_L = X_C$) & the error = 0

Error (iii) \rightarrow can be corrected by measuring
reducing the coupling betⁿ the watt.

Error (iv) \rightarrow can be corrected by connect-
ing the Pressure coil across the
Supply & current coil in series with
the load.

v) \rightarrow can be corrected by using stranded
conductors to minimize ~~error~~ the eddy
current flowing in the current coil
itself.

vi) can be corrected by proper
shielding i.e. the watt meter must
be properly shielded to reduce the
magnetic effect.

vii) The vibration, frictions can be reduc-
ed by using light weight moving
system.

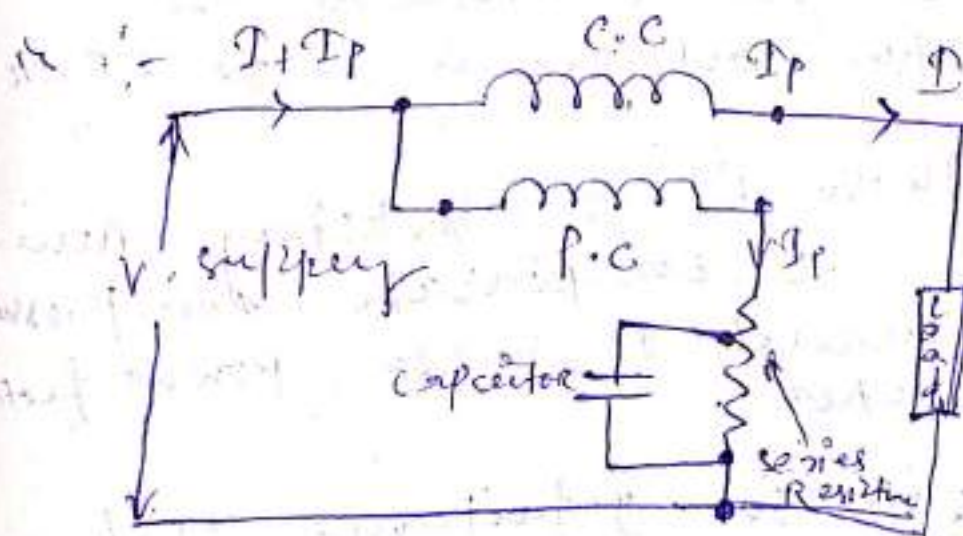
viii) The temperature rise can be
corrected by using copper or resistance
alloy which has temp. coefficient of
1:10.

Low Power Factor wattmeter (Electro-dynamic meter type)

Measurement of power in circuit having low power factor by ordinary electro-dynamometer wattmeter is difficult and inaccurate because:-

- i) The deflecting torque on the moving system is small even when the current & pressure coil are fully excited
- (ii) error introduced because of inductance of pressure coil tend to be large at low power factor.

Special features or compensations in electro-dynamic meter wattmeter



Low power factor wattmeter

1) Pressure coil current!

Pressure coil ~~current~~ circuit is design to have low value resistance, so that the current, flowing through it is increased to give an increased operating torque. The pressure coil current in a low power factor wattmeter may be as much as 10 times the value employed for high power factor.

Compensate for Pressure coil!

The power being measured in a low power factor circuit small & current is high on account of low power factor cannot be used because large load current there would be large power loss in the current coil & therefore the wattmeter will give a large error.

→ There is absolutely necessary to compensate for pressure coil current in a low power factor wattmeter.

Compensate for inductance coil

→ In a low power factor wattmeter we must compensate for the error caused by inductance of the pressure coil. This is done by connecting a capacitor across
(Power Factor)

a part of series resistance in the pressure coil circuit.

Small control torque : - low power factor wattmeter core design with to have a small control torque so that they give full scale deflection ~~at~~ for power factor.

CHAPTER - 04

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1- ϕ Energy meter Induction type

→ The power delivered over a period of time, called energy.
Energy = $\int v i \cos \phi dt$

→ There are 4 main parts of single ϕ energy meter.

- (I) Driving system
- (II) Moving system
- (III) Braking system
- (IV) Registering system or Recording.

(I) Driving system:-

The driving system consist of 2 electro magnet

- (i) shunt magnet
- (ii) series magnet

→ The core of these electro magnet is made up of silicon steel lamination.

→ The coil of both of the electromagnet is excited by load current.

→ Hence the coil is called as current coil.

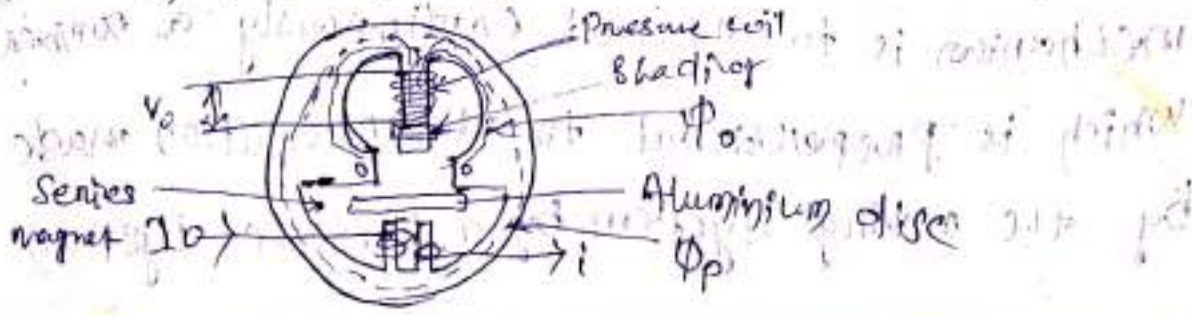
→ The coil of second electromagnet is connected across the supply, and the coil carry a current proportional to supply voltage.

→ The coil is known as pressure coil.

Copper shading bands are provided on the central limb.

→ The position of these band is adjustable.

→ This band is used to bring the flux produced by the shunt magnet exactly in quadrature with the applied voltage.



Moving system:

→ It consists of aluminium disc: The disc is cased in betⁿ series and shunt magnet.

→ The upper part of moving system is a steel pin located in a hole in the bearing cap, fix to the shaft.

→ Hence the rotating shaft has a small magnet at each end where the copper magnet of the shaft is attracted to a magnet in the upper bearing.

→ The moving system thus floats without touching either bearing surface.

Bearing system:

→ A permanent magnet position near the edge of the aluminium disc moves in the field of disc magnet and thus provides a braking torque. can be adjusted by shifting the permanent magnet to different radial positions.

Registering mechanism:

The function of a registering or counting mechanism is to record continuously a number which is proportional to the revolution made by the moving system by a suitable system

a train of reduction gear the pinion of the motor shaft drives a series of five or six pointers. These rotate on round dials which have markings with ten equal divisions.



Testing of Energy meters

The term or 'testing' includes the checking of the actual registration of the meter as well as the adjustment done to bring the error of the meters within the prescribed limits.

Part C Energy meters :-

Meters should be tested for following conditions.

- 1) At 1 Percent of marked current with unity power factor.
- 2) At 100 or 125 Percent of marked current with unity power factor.
- 3) At the one intermediate load with unity power factor.
- 4) At marked current and 0.5 lagging power factor.

Adjustment of single- ϕ energy meter

Some adjustments are carried on energy meters so that they correctly & their errors are within allowable limits.

The sequence of the adjustments are :-

(1) Preliminary light load adjustment :-

The Rated voltage is applied to the potential coil with no current through the current coil.

The light load device is adjusted until the disc just ~~to~~ starts to start.

full load unity factor adjustment

The pressure coil is connected across the rated supply voltage and rated full load current at unity power factor is passed through the coil. The position of the brake magnet is adjusted to vary the braking torque so that the meter revolves at the correct speed within required limits of error.

5) Lag adjustment :- (L.P.F. adjust)

The pressure coil is connected across rated supply voltage and rated full load current is passed through the current coil at 0.5 p.f lagging. The lag device is adjusted till the meter runs at correct speed.

(7) Creep adjustment

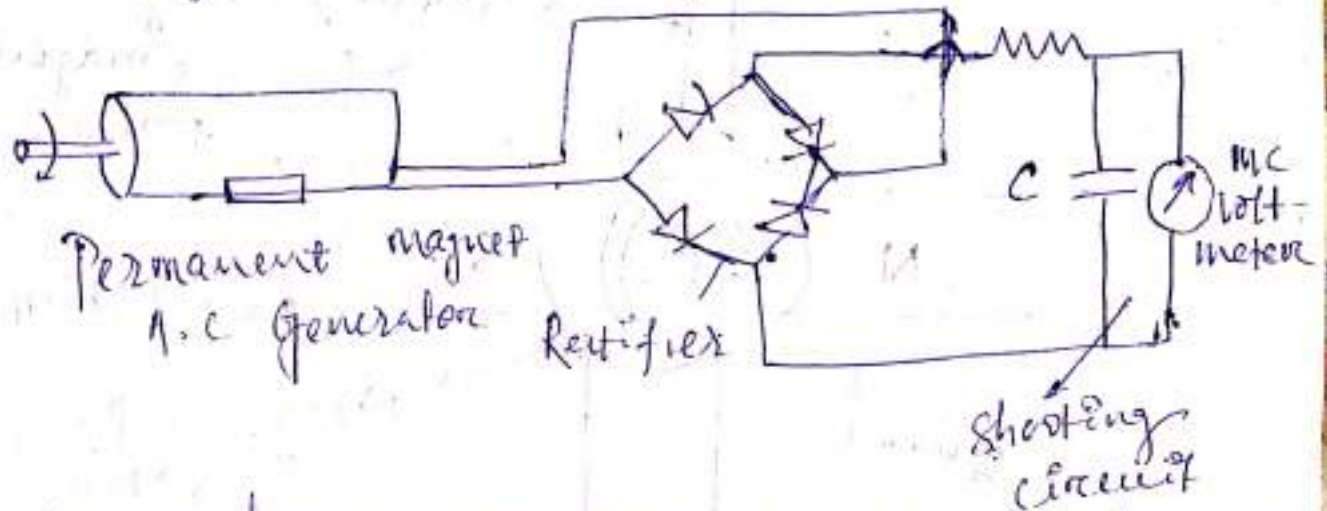
As a final check on light load adjustment, the pressure coil is excited by 110 percent of rated voltage with zero load current. If the light load adjustment is correct, the meter should not creep under these conditions.

EFF.

CHAPTER - 05

Measurement of Speed frequency Power factor Meter

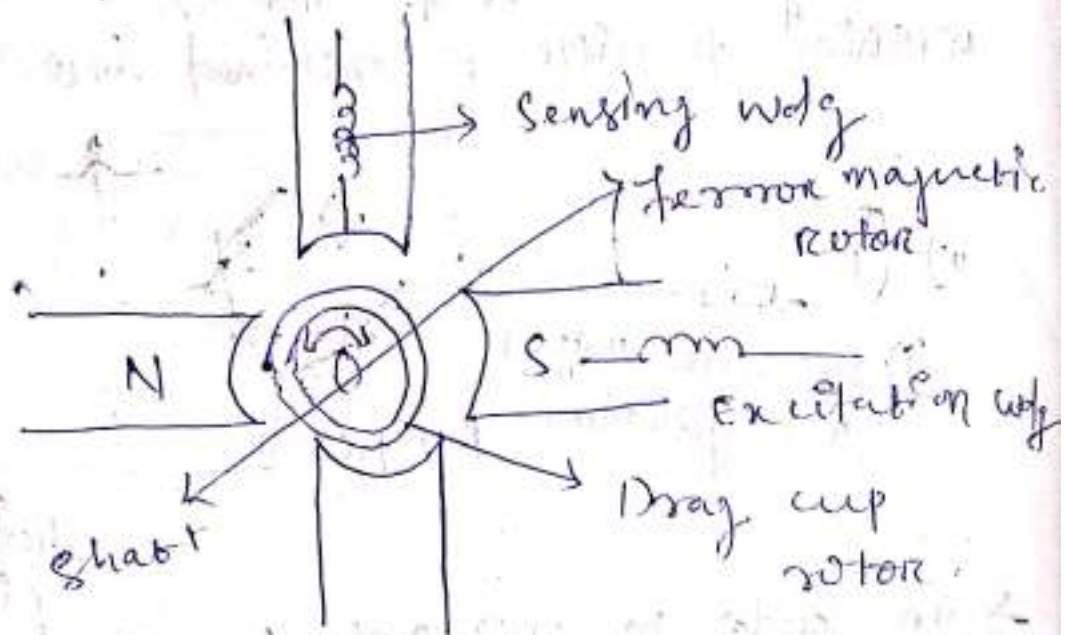
Tachometer is an instrument to measure the rotating speed of d.c. ~~ms~~ m/c or a.c. m/c. The working principle is explained below.



→ In order to overcome some of the difficulties mentioned above i.e. due to maintenance problem brush contact, commutator etc. d.c. tachogenerator have rotating magnet which may be either a Permanent magnet, or an electro magnet. The coil is wound on the stator.

→ The rotation of magnet causes an e.m.f. to be induced on the stator coil. The amplitude & frequency of this e.m.f. are both proportional to the speed of rotation. Thus ~~and~~ either amplitude or frequency of induced voltage is used as a measure, the o/p voltage of a.c. tachogenerator is rectified and is measured with a permanent magnet. moving coil

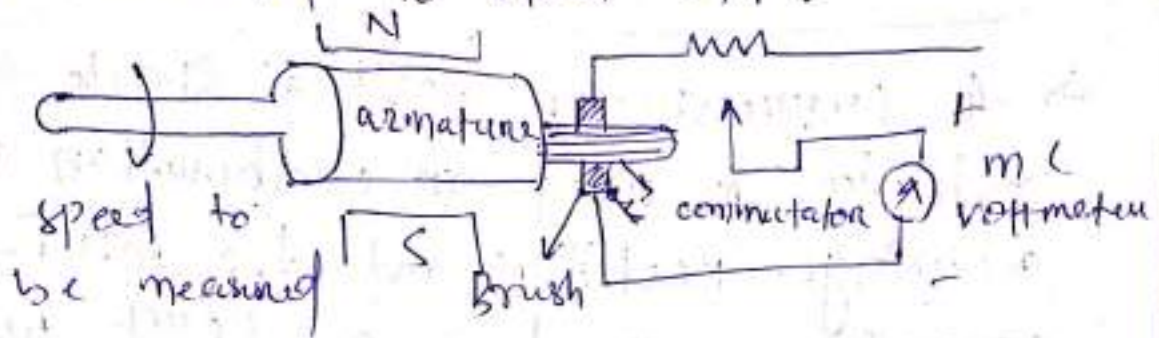
→ In case of drag cup type Rotor AC Tacho generator there are two winding i.e. Excitation wdg and Sensing wdg



→ The rotor is very light & highly conducting and acts as S.C wdg. A low reluctance path is provided. The rotation of rotor causes an induced voltage in the sensing wdg & this voltage is proportional to the inst. value of speed. The excitation frequency is very large as compared with speed.

→ DC Tachogenerator is transducer which is used to measure the angular speed of the rotating m. i. c.

→ The angle (θ) of the angular shaft is converted to elect o/p.



Working Principle

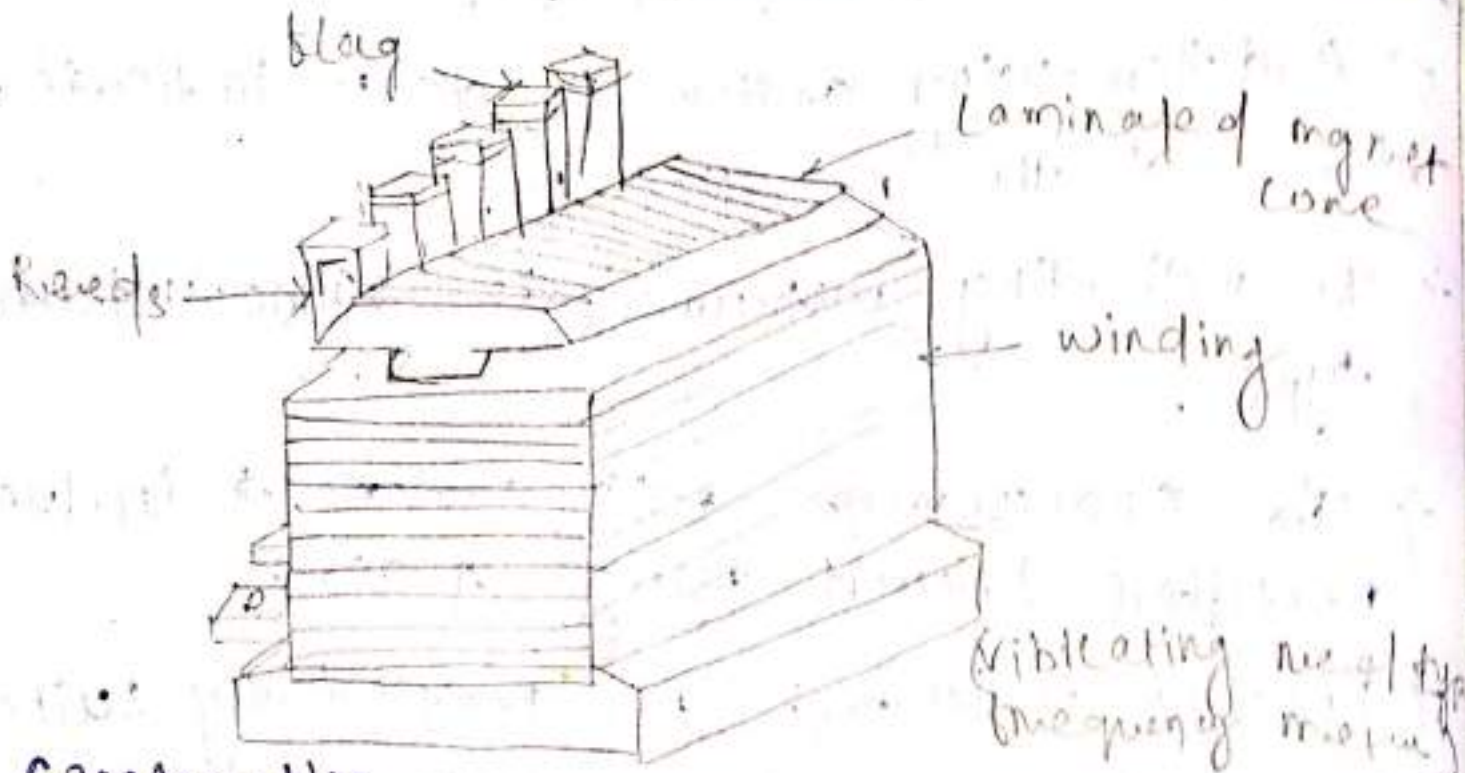
Consider two permanent magnetic poles N and S inside which an armature is placed. A commutator is connected to the armature whose speed is to be measured.

The angular speed of the shaft can be measured by comparing the elect. o/p of them m/c

$$N \propto E_o$$

The advantage of this transducer is 10mV/Rev sensitivity & can be measured with the m.c. voltmeter.

Mechanical Resonance type frequency meter



Construction

- This meter consists of number of thin steel strips called reeds.
- The reeds are placed in a row and closed to an electromagnet.
- The electromagnet has a laminated iron core and its coil is connected in series with a resistance across a supply whose frequency is to be measured.

→ These reeds are approximately about 9 millimetre wide and 0.5 mm thick.

→ All reeds are not exactly similar to each other.

→ The natural frequency of vibration of the reeds depends upon their weight and dimension.

Since the reeds have different weight and sizes their natural frequency of vibration are different.

→ The reeds are arranged in ascending order of natural frequency.

→ The difference in frequency is usually 0.5 Hz.

→ So the natural frequency of 1st reed may be 1 Hz.

→ The flags are painted white to get a good max. contrast against their black background.

→ When the frequency meter is connected across the supply whose frequency is to be measured, the coil of electro magnet carries a current i , which alternate at the supply frequency. The force of attraction betⁿ the reeds and the electromagnet is proportional to i^2 so these force varies at twice the supply frequency.

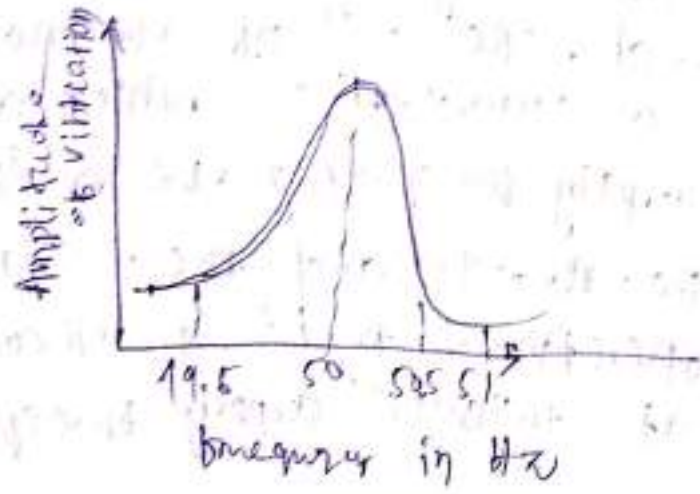
→ So the bar is excited on the resonance. Varies every half cycle, all the threads will tend to vibrate. But the thread whose natural frequency is equal to twice the frequency of supply will be in resonance and will vibrate most.

Advantages:

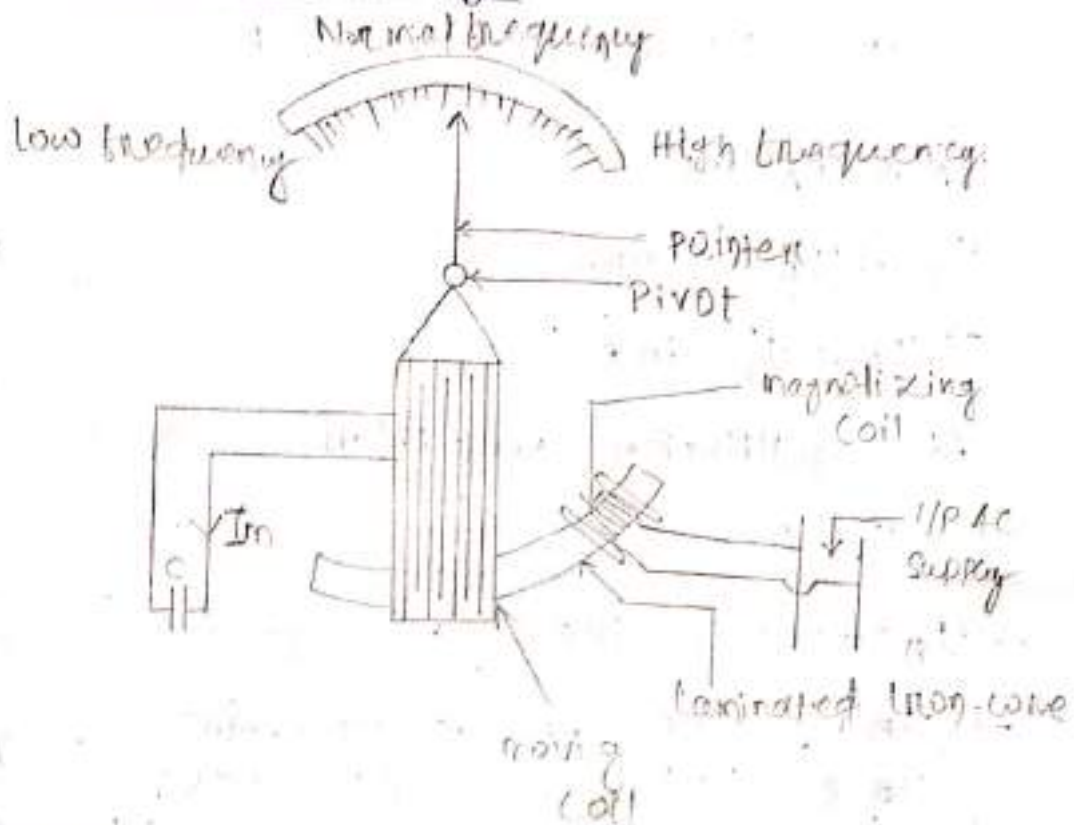
- The indication is virtually independent of the waveform of supply voltage.
- The indication is independent of magnitude of applied voltage also provided the voltage is not too low.

Disadvantages:

- Such instrument can not be read much closer than half the frequency difference between adjacent threads.
- The reliability of reading also depends upon the accuracy with which the metal reading have been tuned.



Electrical Resonance type :-



Principle :-

The working principle of this instrument is based on the working principle of resonance in a R, L, C circuit.

Construction :-

- It consists of a fixed coil which is connected across the supply. ~~the~~ whose frequency should be measured.
- This coil is also called as magnetising coil.
- The magnetising coil is mounted on a laminated iron core.
- The moving coil is attached with a spindle which is pivoted on the bearing which is allowed to move freely.

→ A pointer fixed with spindle which moves over a calibrated scale: and a capacitor of suitable value is connected across the moving coil.

Working:—

→ The fixed coil draws a current I and this current produces a flux ϕ . If we neglect the resistivity of the coil, and iron loss

in the core flux ϕ is in phase with current I . This flux ϕ being alternating in nature, produces an

emf E and this emf lags behind the flux by 90° .

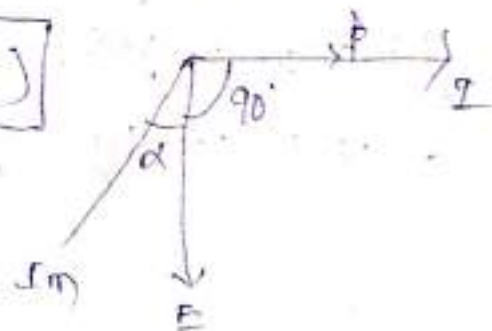
The emf induces a current I_m in the moving coil.

1st case

The circuit of the moving coil is assumed to be inductive. Then the current I_m lags behind the emf E by an angle α .

The torque acting on the moving coil is

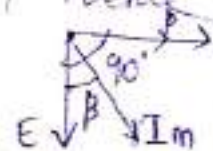
$$T_d \propto I_m \cos(90^\circ + \alpha)$$



Case 2

The moving coil is assumed to be purely capacitive. Then the current I_m leads the emf E by an angle β . and therefore the deflecting torque is

$$T_d \propto I_m \cos(90^\circ - \beta)$$

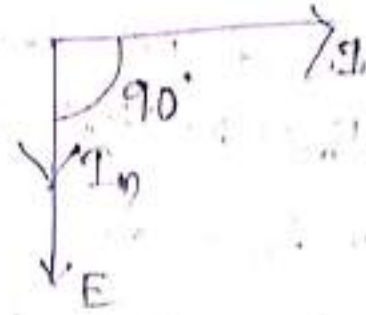


Case III

The inductive reactance is support of ϕ be equal to the capacitive reactance, then some ϕ is under resonance condition, ($X_L = X_C$)
So the moving coil ϕ is purely resistive and I_m is in phase with E .

$$I_d \propto I_m \cos 90^\circ = 0$$

$$I_d \propto I_m$$



The pointer does not move or the pointer is act as equilibrium when, $X_L = X_C$.

For high frequency $X_L > X_C$

For low frequency $X_C < X_L$

Advantage:

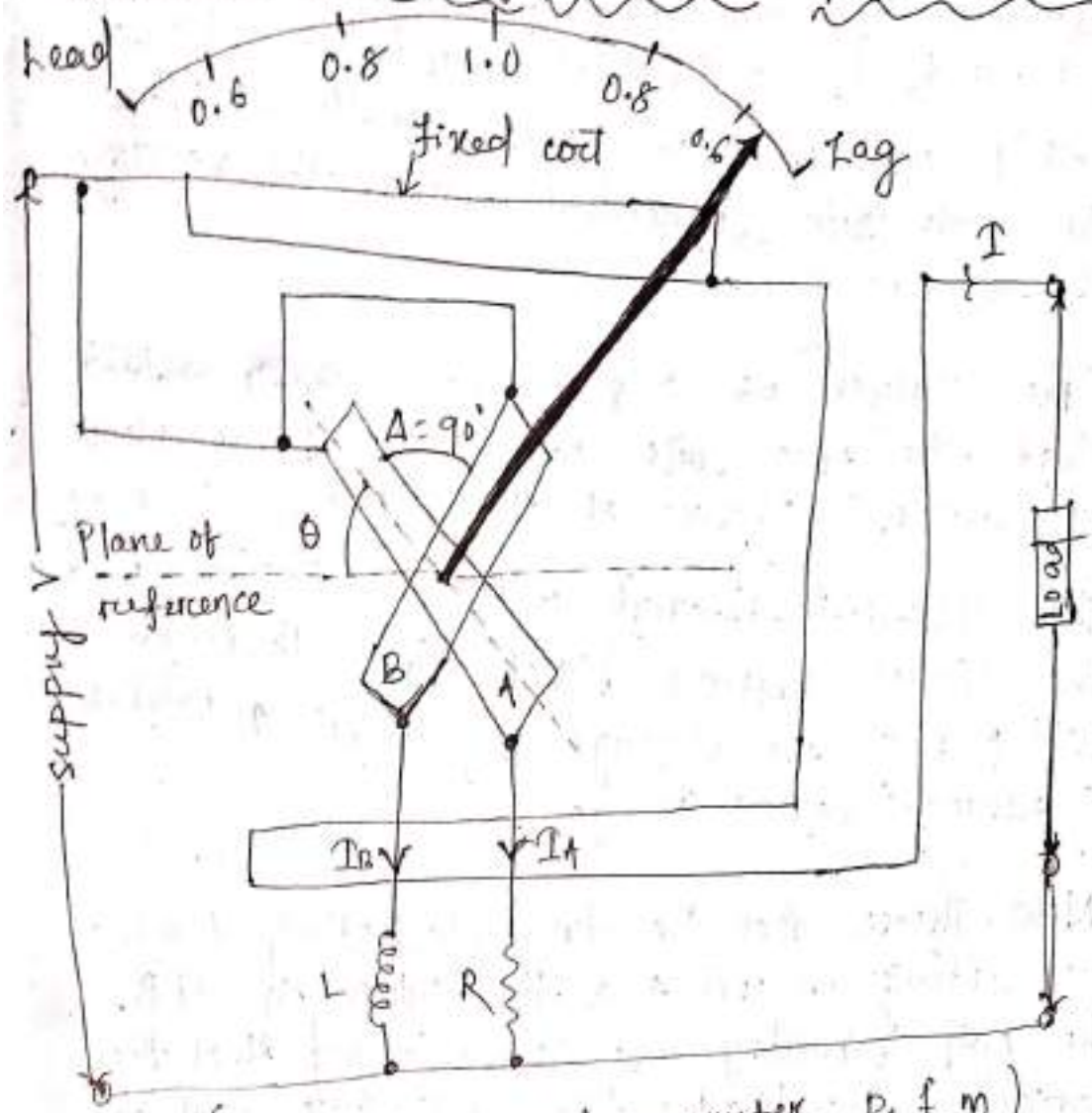
→ It is highly sensitive

→ It can be used for measurement of wide range of frequency.

Disadvantages:

→ It is costly.

Single- ϕ Electrodynamometer Power Factor Meter



(Single- ϕ electrodynamometer p. f. m)

- It consists of fixed coil which acts as the current coil. This coil is split up into two parts and carries the current of the circuit under test.
- Therefore, the magnetic field produced by this coil is proportional to the main current.
- Two identical pressure coil A & B pivoted on a spindle constitute the moving system.
-

→ Presence coil A has a non inductive resistance R connected in series with it, and coil B has a highly inductive choke coil 'L' connected in series with it. The two coils are connected across the voltage V of the circuit.

→ The values of R & L are so ~~adjusted~~ adjusted that the two coils carry the same value of current at normal frequency i.e. $R = \omega L$.

→ The current through coil A is in phase with the circuit voltage while that through coil B lags the voltage by angle θ which is nearly equal to 90° .

→ Now, there will be two deflecting torque one acting on coil A & the other on coil B. The coil winding are so arranged that the torque due to the two coils are opposite direction. Therefore the pointers will take up a position where these two torques are equal.

→ Let us consider in the case of lagging power factor of $\cos \phi$.

Deflecting torque acting on coil A is -

$$T_A = kVI M_{\max} \cos \phi \sin \alpha$$

where α : angular deflection from the plane of reference,

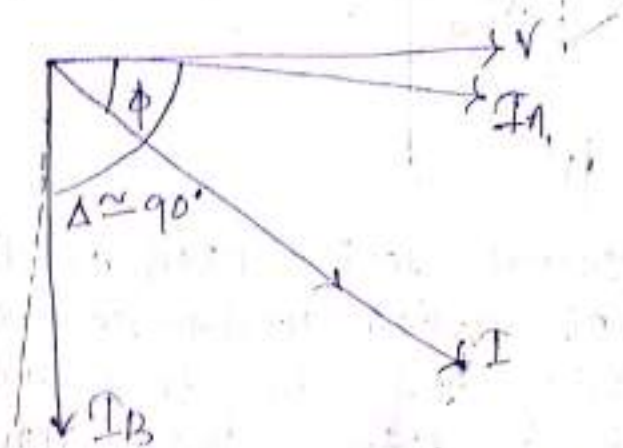
and M_{\max} : maximum value of mutual inductance between the two coils.

This torque says acts in the clockwise direction.

→ Deflecting torque acting on coil B is:-

$$T_B = kVI M_{\max} \cos(90^\circ - \phi) \sin(90^\circ + \theta)$$

$$= kVIM_{\max} \sin \phi \cos \theta$$



The coils will take up such a position that the two torques are equal.

Hence at equilibrium $T_A = T_B$

$$\text{or, } kVIM_{\max} \cos \phi \sin \theta = kVIM_{\max} \sin \phi \cos \theta$$

$$\text{or, } \theta = \phi$$

Therefore the deflection of the instrument is measure of phase angle of the circuit.

The scale of the instrument can be ~~calibrated~~ calibrated directly in terms of power factor.

$$\cos \phi \cdot \sin \theta = \sin \phi \cdot \cos \theta$$

$$= \frac{\sin \theta}{\cos \theta} = \frac{\sin \phi}{\cos \phi} \Rightarrow \tan \theta = \tan \phi$$

$$= \boxed{\theta = \phi}$$

CHAPTER - 06

Classification of Resistor :-

- Low resistance $R \leq 1$
- medium resistance $1 < R < 100k$
- High resistance $R > 100 \Omega$

Low Resistance :-

All resistances of the order 1Ω or less than 1Ω are classified as low resistance.

Eg \rightarrow series field resistance, Ammeter

Medium Resistance :-

This class include resistance from 1Ω to $100k \Omega$.

Eg - shunt field resistance, incandescent lamp.

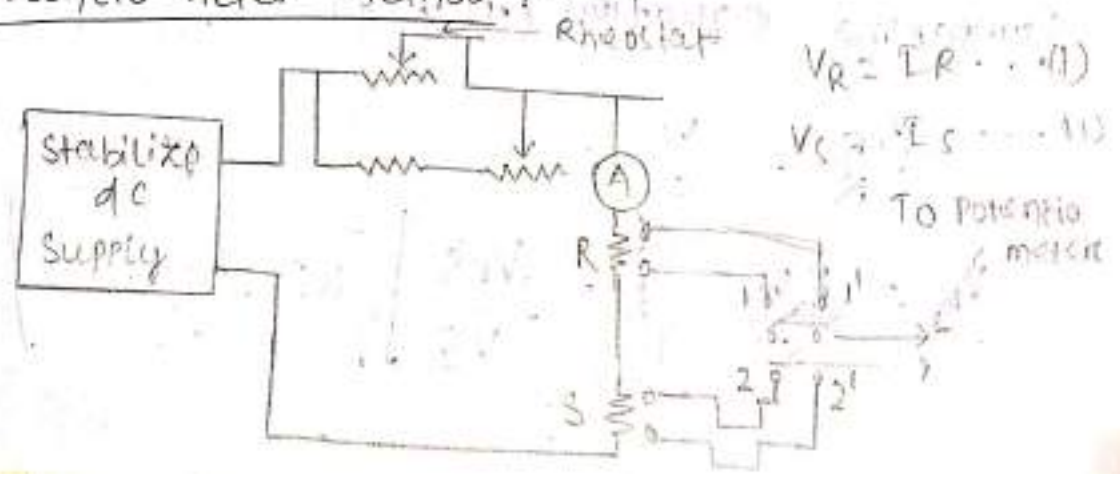
High resistance :-

Resistance of the order $100k \Omega$ and upward are classified as high resistance.

Eg - insulation resistance.

Measurement of low Resistances :-

Potential meter method :-



R is a unknown resistor which is connected in series with the standard resistor S . The current through the circuit is controlled by the rheostat.

→ A 2 pole double throw switch is used in the circuit. When this switch is put in position 1 and it connects to the unknown resistance to the potentiometer.

Suppose the reading of the potentiometer is $V_R = IR \dots (1)$

$$I = \frac{V_R}{R} \dots (2)$$

Now again the switch put in the position of 2 & it connects standard resistance to the potentiometer.

So the reading of the potentiometer is $V_S = I_S \dots (3)$

$$I = \frac{V_S}{S} \dots (4)$$

Comparing equation (2) & (4)

$$\frac{V_R}{R} = \frac{V_S}{S}$$

$$V_R = \frac{R V_S}{S} \quad \boxed{R = \frac{V_R S}{V_S}} \quad \boxed{R = \frac{V_R}{V_S} \cdot S}$$

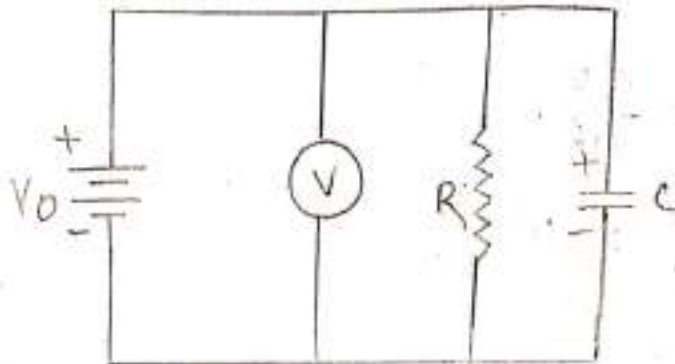
Since the value of standard resistance R_s is known, the value of R can also be known.

This method is suitable for low resistance.

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NO Measurement of High Resistance :-

Loss of charge Method :-



In this method the insulation resistance R is measured, which is connected in parallel with a capacitor C and an electrostatic voltmeter.

The capacitor is charged by means of a battery, having voltage V_0 . Then the capacitor is allowed to discharge through the resistance.

The current through the capacitor at time T second

$$i = -\frac{dq}{dt} \quad \text{--- (1)}$$

$$i = \frac{V}{R} \quad \text{--- (2)}$$

$$\text{Now } q = CV \quad dq = C dV$$

Putting the value of q in eqn (1)

$$i = -c \frac{dv}{dt} \quad \text{--- (11)}$$

Again

$$i = \frac{V}{R} \quad \text{--- (10)}$$

from eqn 2 & 3

$$\frac{V}{R} = -c \frac{dv}{dt}$$

$$\Rightarrow \frac{V}{Rc} = -\frac{dv}{dt}$$

$$\Rightarrow \frac{V}{Rc} + \frac{dv}{dt} = 0$$

Let $\frac{d}{dt} = D$

$$\frac{V}{Rc} + DV = 0$$

$$\Rightarrow V \left(\frac{1}{Rc} + D \right) = 0$$

$$\Rightarrow \left(\frac{1}{Rc} + D \right) = 0$$

$$= \boxed{D = -\frac{1}{Rc}}$$

C.F.

$$V = C.F. + P.I$$

$$C.F. = k e^{\frac{D}{Rc} t} = k e^{-\frac{1}{Rc} t}$$

$$= k e^{-\frac{t}{Rc}}$$

$$P.I = 0$$

$$V = C.F + P.I = k e^{-t/Rc} \dots \dots (4)$$

At $t=0$

$$\text{Now let } t=0 \quad V=V_0$$

$$[e^0=1]$$

$$V_0 = k e^{-0/Rc} \Rightarrow \boxed{V_0 = k}$$

By putting the value of k in eqn (4)

we get

$$V = V_0 e^{-t/Rc}$$

$$\Rightarrow \frac{V}{V_0} = e^{-t/Rc}$$

Taking log on both side

$$\log \frac{V}{V_0} = \log e^{-t/Rc}$$

$$[\log \frac{a}{b} = \log a - \log b]$$

$$= \ln V - \ln V_0 = -\frac{t}{Rc} \log e \quad [\log_{10} x = \ln x]$$

$$[\log e^n = n \log e]$$

$$= -\frac{t}{Rc}$$

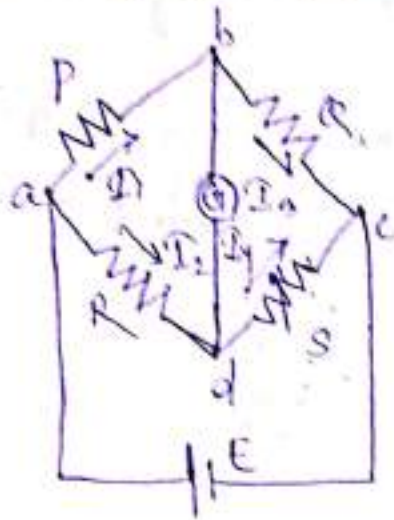
$$[\log e = 1]$$

$$\times \log(\ln V_0 - \ln V) = \frac{t}{Rc}$$

$$\Rightarrow \ln V_0 - \ln V = \frac{t}{Rc}$$

$$\boxed{R = \frac{1}{C} \cdot \frac{t}{\ln \frac{V_0}{V}}}$$

Measurement of Medium Resistance by Wheatstone bridge method :-



→ A very important device used in the measurement of medium resistances is the Wheatstone Bridge. A Wheatstone bridge has been in use longer than almost any electrical measuring instrument.

→ It has four resistive arms, consisting of resistances P, R, S and X together with a source of emf, usually a galvanometer 'G' or other sensitive current meter.

→ For bridge balance, we can write,

$$I_1 P = I_2 R \quad \text{--- (i)}$$

For the galvanometer current to be zero, the following conditions also exist :-

$$I_1 = I_3 = \frac{E}{P+R} \quad \text{--- (ii)}$$

$$\& I_2 = I_4 = \frac{E}{R+S} \quad \text{--- (iii)}$$

where E = emf of the battery.

combining eqⁿ 1, 2, & 3 and simplifying we obtain -

$$\frac{P}{P+Q} = \frac{R}{R+S} \quad \text{--- (4), } PR + PS = \cancel{PR} + \cancel{QR}$$

from which $QR = PS$ --- (5)

equation (5) is the well known expression for the balance of wheatstone bridge. If three of the resistances are known, the fourth may be determined from eq - (5) we obtained: -

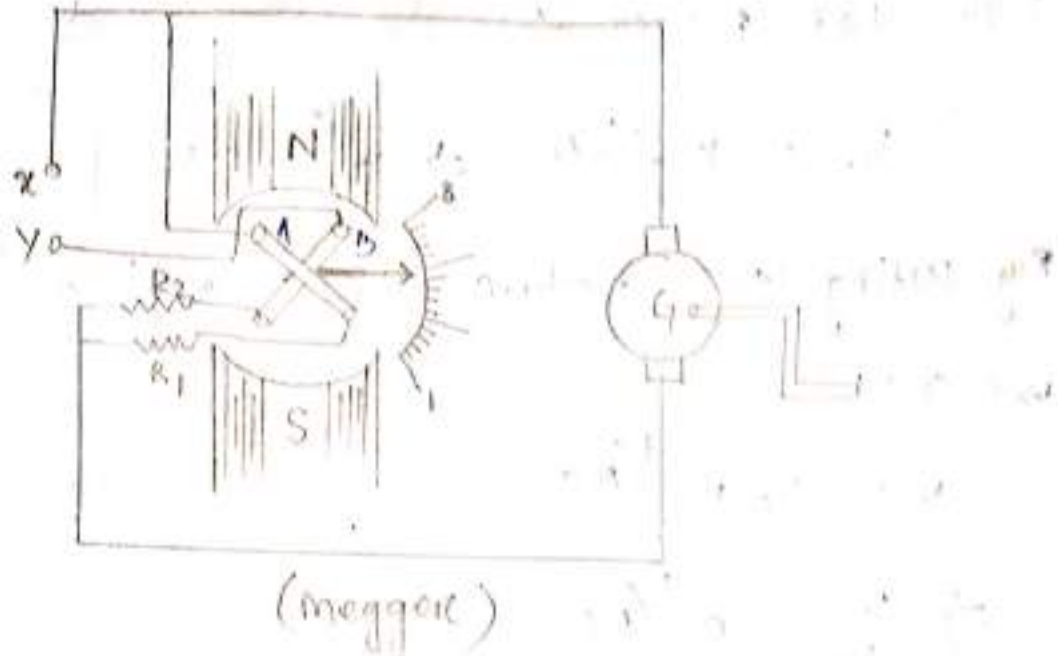
$$R = S \cdot P / Q$$

where 'R' is the unknown resistance, 'S' is called the 'standard arm' of the bridge and 'P' & 'Q' are called the 'ratio arms'

- 0 - (6)

Meggers

Meggers are the instrument which measure the electric insulation resistance of the electrical circuit.



Construction :-

It consists of a hand driven dc generator and an ohm meter. The ohm meter consists of a coils A and B.

→ The pointer is attached to the spindle which moves over a calibrated scale.

→ The two coils are kept inside a permanent magnetic field.

→ Let R_1 & R_2 be the resistance of the coil A and B.

→ The terminal X & Y are used to connect the resistance whose value measured.

Let I_A = current in the coil A

I_B = current in the coil B

$$T_A \propto I_A \cos \theta$$

$$T_B \propto I_B \cos (90 - \theta)$$

$$\Rightarrow T_B \propto I_B \sin \theta$$

At equilibrium condition

$$T_A = T_B$$

$$\Rightarrow I_A \cos \theta = I_B \sin \theta$$

$$\Rightarrow \frac{I_A}{I_B} = \frac{\sin \theta}{\cos \theta} = \tan \theta$$

$$\theta = \tan^{-1} \left(\frac{I_B}{I_A} \right)$$

$$= \tan^{-1} \left(\frac{V/R_1}{V/R_2} \right)$$

$$\theta = \tan^{-1} \left(\frac{R_2}{R_1} \right)$$

$$\frac{I_A}{I_B} = \frac{\sin \theta}{\cos \theta} = \tan \theta$$

$$\theta = \tan^{-1} \left(\frac{I_A}{I_B} \right)$$

$$= \tan^{-1} \left(\frac{V/R_1}{V/R_2} \right) = \theta = \tan^{-1} \left(\frac{R_2}{R_1} \right)$$

By knowing the value of angle θ , R_1 and R_2 will be found out.

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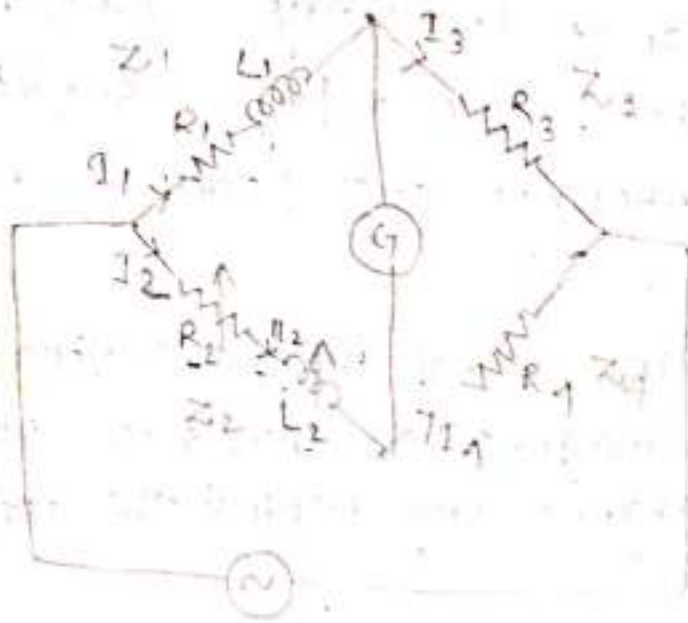
Frequency meters:-

It is of two type.

(1) mechanical

(2) Electrical Resonance type

Maxwell's variable inductance Bridge :-



The value of

$$R_1 = R_1$$

$$L_1 = j\omega L_1$$

$$C_1 = \frac{1}{j\omega C_1}$$

Let L_1 is the unknown inductance
 R_1 is the unknown resistance
 R_2 is the variable resistance
 L_2 is the variable inductance with internal resistance π_2
 R_3 & R_4 is the known resistances

At balance condition :-

$$Z_1 Z_4 = Z_2 Z_3$$

$$\Rightarrow (R_1 + j\omega L_1) R_4 = (R_2 + \pi_2 + j\omega L_2) R_3$$

$$\Rightarrow R_1 R_4 + j\omega L_1 R_4 = R_2 R_3 + R_3 \pi_2 + j\omega L_2 R_3$$

$$\Rightarrow R_1 R_4 - R_2 R_3 - R_3 \pi_2 = j\omega L_2 R_3 - j\omega L_1 R_4$$

$$R_1 R_4 - R_2 R_3 - R_3 r_2 = 0$$

$$\Rightarrow R_1 R_4 = R_3 (R_2 + r_2)$$

$$R_1 = \frac{R_3 (R_2 + r_2)}{R_4}$$

$$j\omega L_2 R_3 - j\omega L_1 R_4 = 0$$

$$j\omega L_2 R_3 = j\omega L_1 R_4$$

$$j\omega (L_2 R_3 - L_1 R_4) = 0$$

$$(L_2 R_3 - L_1 R_4) = 0$$

$$L_1 = \frac{L_2 R_3}{R_4}$$

$$P_d = I A \cos \theta$$

$$P_d = I B \sin \theta$$

$$\cos(90^\circ - \theta)$$

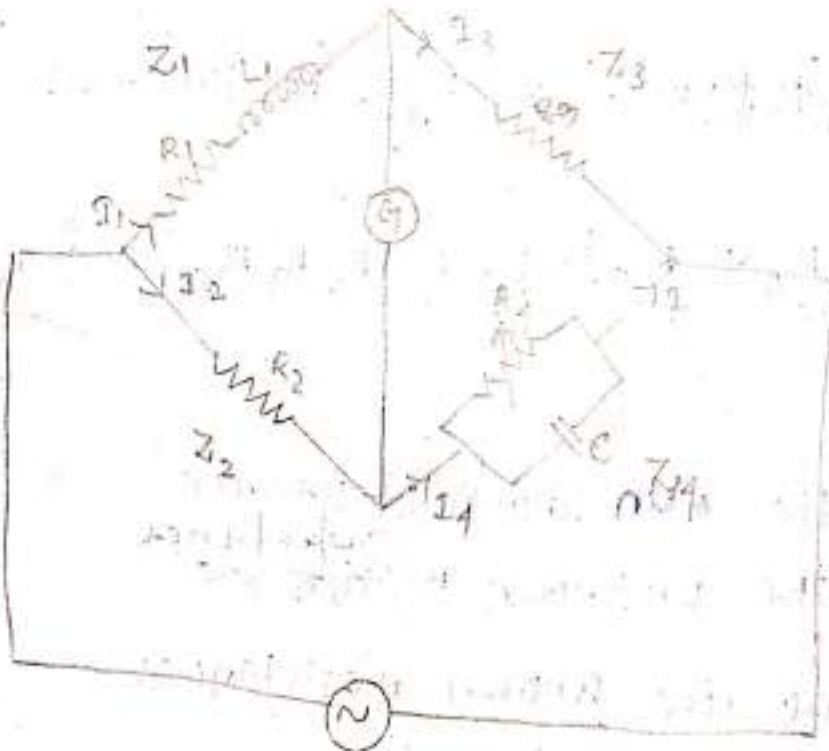
$$\sin \theta$$

$$\frac{\cos \theta}{\sin \theta} =$$

$$\theta = \left(\frac{L_2}{R_4} \right) \left(\frac{1}{R_1} \right) \left(\frac{1}{R_2} \right)$$

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Maxwell's inductance & capacitance Bridge :-



At balance condition:-

$$Z_1 Z_4 = Z_2 Z_3$$

$$\Rightarrow (R_1 + j\omega L_1) \left(\frac{R_4 X_c}{R_4 + X_c} \right) = R_2 R_3$$

$$= (R_1 + j\omega L_1) \left(\frac{R_4 \frac{1}{j\omega c}}{R_4 + \frac{1}{j\omega c}} \right) = R_2 R_3$$

$$= (R_1 + j\omega L_1) \left(\frac{\frac{R_4}{j\omega c}}{\frac{R_4 j\omega c + 1}{j\omega c}} \right) = R_2 R_3$$

$$= (R_1 + j\omega L_1) \left(\frac{R_4}{R_4 j\omega c + 1} \right) = R_2 R_3$$

$$= R_4 (R_1 + j\omega L_1) = R_2 R_3 (R_4 j\omega c + 1)$$

$$= R_1 R_4 + R_4 j\omega L_1 = R_2 R_3 R_4 j\omega c + R_2 R_3$$

Let

R_1 is the ~~un~~ known resistance

L_1 is the unknown ^{inductance} ~~resistance~~

$R_2 R_3$ are the known resistances

$R_4 c$ are the variable resistance & capac

$$\Rightarrow R_1 R_4 - R_2 R_3 = R_2 R_3 R_4 j\omega C - R_1 j\omega L_1$$

$$R_1 R_4 - R_2 R_3 = 0$$

$$R_1 R_4 = R_2 R_3$$

$$\boxed{R_1 = \frac{R_2 R_3}{R_4}}$$

$$R_2 R_3 R_4 j\omega C - R_1 j\omega L_1 = 0$$

$$R_2 R_3 R_4 j\omega C =$$

$$R_1 j\omega (R_2 R_3 - L_1) = 0$$

$$\Rightarrow R_2 R_3 C - L_1 = 0$$

$$\Rightarrow \boxed{L_1 = R_2 R_3 C}$$

Quality factor:-

Quality factor is the ratio of the inductance to resistance.

$$Q = \frac{\omega L_1}{R_1} = \frac{\omega (R_2 R_3 C)}{\frac{R_2 R_3}{R_4}} = \frac{\omega R_3 C}{R_4} = \omega C R_4$$

$$\boxed{Q = \omega C R_4}$$

Advantages:-

- The 2 balance equations are independent if we chose R_1 & C as variable element.
- The frequency does not appear in any one of 2 eqⁿ.

Disadvantage:-

- This bridge required a variable standard capacitor which may be very expensive.
- The bridge is limited to measurement of low quality factor.

CHAPTER - 07

Sensor and transducer

- Transducer** - Transducer is a device which converts the energy from one form to another, (convert mechanical force into electrical signal) Ex: used in industrial instrumentation etc.
- * An electronic instrumentation system consists of a no. of components to perform a measurement and record its results.
 - * In general measurement system consists of three major components:
 - a) An input device.
 - b) A signal conditioning or processing device.
 - c) An output device.
 - * The input device receives the measurand or the quantity under measurement and delivers a proportional or analogous electrical signal to the signal conditioning device.
 - * Here the signal is amplified, attenuated, filtered, modulated or modified in such a format, so that it is acceptable by the output device.
 - * The input quantity for most instrumentation system is a "non-electrical quantity". In order to use electrical methods & techniques for measurement, manipulation or control, the non-electrical quantity is generally converted into an electrical form by a device called a "transducer". (***)
 - * Example - Mobile phone - (converts the sound into electrical signals and then amplifies it into the preferred range. Then, alters the electrical signals into audio signals at the o/p of the speaker.
 - * Transducer contains two important parts:
 - a) sensing or detector element.
 - b) Transduction element.
- Sensing or Detector Element** - A detector or a sensing element is that part of a transducer which responds

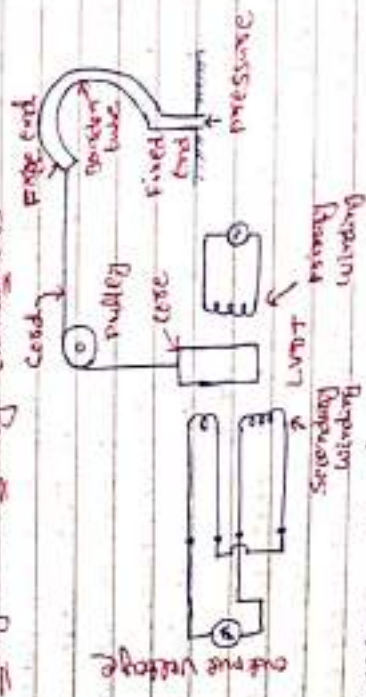
to a physical phenomenon or a change in a physical phenomenon.

- * Here the response of the sensing element must be closely related to the physical phenomenon.
- * Transduction element:
- * A transduction element transforms the output of a sensing element to an electrical output.
- * Here the transduction element, in a way acts as a secondary transducer.

Classification of transducers

- * The transducers can be classified on the basis of transduction form used (analog, digital, etc.)
- * As primary and secondary transducers.
- * As passive and active transducers.
- * As analog and digital transducers.
- * As transducers and inverse transducers.

Primary & secondary transducers



- * Consider a Bourdon's tube, which is set up as shown in figure above.
- * This tube acting as a primary detector senses the pressure and converts the pressure into a displacement at its free end side.
- * The displacement of the free end moves the

analogous -> comparable in certain respects.

case of a linear variable differential transformer (LVDT) which produces an output voltage.

- * This voltage is proportional to the movement of a core, which is proportional to the displacement of the free end & is proportional to the pressure.
- * Here two stages of transduction occurred. Firstly the pressure is converted into a displacement by Bourdon tube then the displacement is converted into an analogous voltage by LVDT.
- * The Bourdon tube is called a "primary transducer" while the LVDT is called a "secondary transducer".
- * LVDT - The linear variable differential transformer is a type of electrical transformer used for measuring linear displacement.

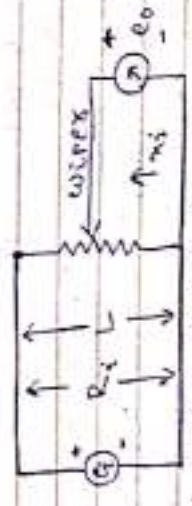
Passive & active transducers

Passive transducers:
Passive transducers require an auxiliary power source for transduction. So it is also called as "externally powered transducers".

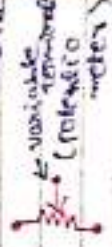
Ex: Passive transducers are resistive, inductive and capacitive transducers.

* Let us take a resistive transducer called "rot" (Linear potentiometer).

* The "rot" is a resistive transducer powered by a source voltage (E_0) and used for measurement of linear displacement (x_i).



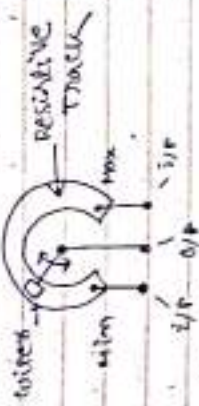
Potentiometer = Variable resistor



* But 'L' is the total length of potentiometer.

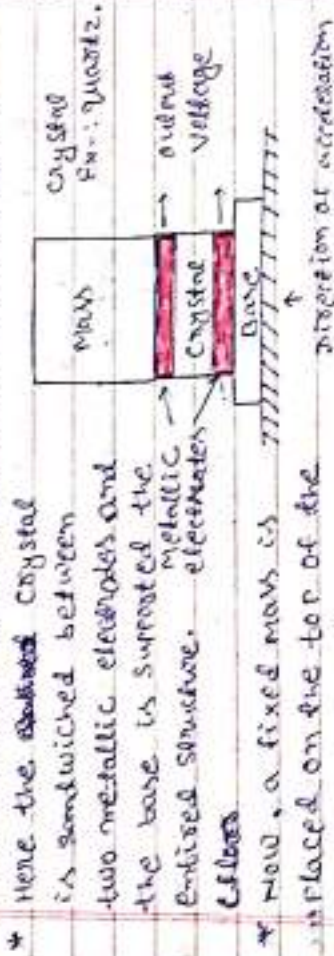
R_i = total resistance
 x_i = input displacement

output voltage $E_o = \frac{r_i}{L} e_i$ or $r_i = \left(\frac{E_o}{e_i}\right) L$



Potentiometer =

- * Used in radio, fan regulator etc.
- * Active transducers.
- * Active transducers are that type of transducers in which an auxiliary power source is not required to produce their output.
- * This type of transducers develop their own voltage or current, hence they are called as self generating type transducers.
- * velocity, temperature, light intensity and force can be transduced with the help of active transducers.
- * Let us take an example of a piezoelectric crystal, which is used for measurement of acceleration.



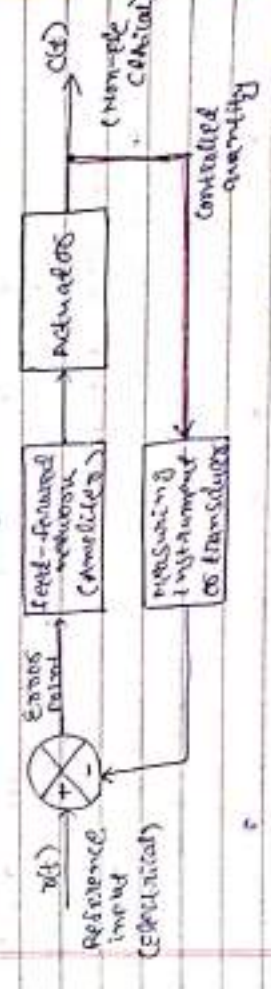
- * Here the ~~quartz~~ crystal is sandwiched between two metallic electrodes and the base is supported the entire structure.
- * Now, a fixed mass is placed on the top of the sandwich crystal.
- * The property of the piezo-electric crystals is that when a force is applied to them, they produce an output voltage. When the acceleration is applied to the base, due to which the mass produces a force and output voltage will be generated.

- * If we fixed the mass, then the force is proportional to acceleration and also to the output voltage.
- * This transducer is called as "accelerometer" which converts acceleration into electrical voltage & does not need any auxiliary power.
- * Analog transducers.
- * These transducers convert the input quantity into an analog output which is a continuous function of time.

- Ex: LVDT, strain gauge, thermistor etc.
- * Thermistor: An electrical resistor whose resistance is produced by heating, used for measurement & control.
- * Continuous function: Small change in input = small change in output.
- * Digital transducers.

- * These transducers convert the input quantity into an electrical output which is in the form of pulses.
- * Discontinuous function: Small change in input = large change in output.
- Ex: Glass scale, Meas. Scale.
- * Transducers: A transducer can be defined as a device which converts a non-electrical quantity into an electrical quantity.

Inverse Transducer: An inverse transducer is defined as a device which converts an electrical quantity into a non-electrical quantity.

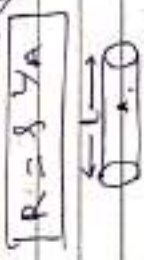


→ Electrical unit signal
→ Mechanical unit signal
(So control is non-electrical quantities)

* output - non electrical signal
 * The controlled quantity is measured & converted into an analogous quantity by transducers which form the feedback loop.
 * The loop input quantity (electrical in nature) is compared with the electrical quantity proportional to the output in a comparator.
 * In this case, the two signals are not equal, so an error signal is produced.

* This error signal is amplified and applied to an actuator in the forward path, which corrects the output quantity till the output quantity reaches the desired level.
 * Controller - a device that causes a machine or other device to operate.
 Resistive transducers -

* Resistive transducers are used to measure the change of resistance because and it is a very suitable method for both the cases. (alternating current & voltage, direct current & voltage).

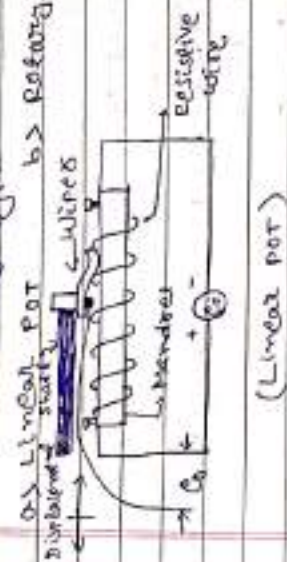


- $R = \text{resistance } (\Omega)$
- $L = \text{length of the conductor (cm)}$
- $A = \text{cross-sectional area of conductor (mm}^2)$
- $\rho = \text{resistivity of conductor } (\Omega\text{-cm})$

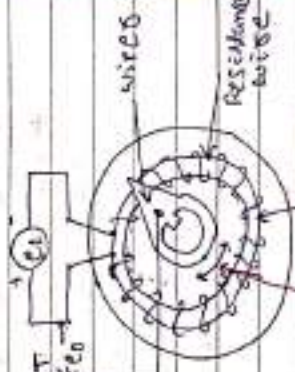
Ex: POT (potentiometer)

* POT consists of a resistive element provided with a sliding contact. This sliding contact is called a wiper.
 * The motion of the sliding contact may be translatory or rotational.
 ↳ the motion in which all the possible of a body move through the same distance in the same time.

* POT are of two type.



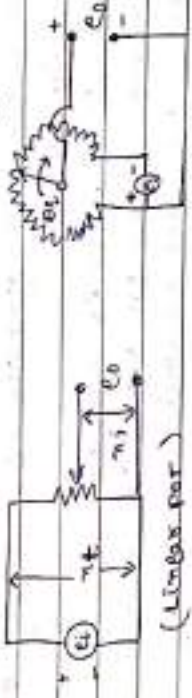
Linear POT
 ↳ Mandrel - a cylindrical rod of metal
 ↳ angular displacement - angular displacement of a body in the angle in radians through which a point revolves around a centre or line has been rotated in a specified sense about a specified axis.
 ↳ a (radian)



Rotational POT
 ↳ Mandrel - a cylindrical rod of metal
 ↳ angular displacement - angular displacement of a body in the angle in radians through which a point revolves around a centre or line has been rotated in a specified sense about a specified axis.
 ↳ a (radian)

* Some pots use the combination of the two motion i.e. translational & rotational.

* These pots have their resistive element in the form of a helix and therefore, they are called helipot.



Helix - it is a type of smooth space curve i.e. a curve in three-dimensional space.
 * The translational resistive elements are straight device (2mm to 0.5m)
 * The rotational devices are circular in shape and are used for measurement of angular displacement.
 * They may have a full scale angular displacement as small as 10°.

- * It may provide accurate measurement upto 357° .
- * Multiturn potentiometers may measure upto 3500° of rotation through use of helipot.
- * It can be used for measurement of either translational or rotary motion.
- * The resistive element of the POT may be excited by either d.c. or a.c. voltage.

Adv. -:

- * They are inexpensive.
- * They are simple to operate and are very useful for measurement of displacement & angular displacement.
- * Their electrical efficiency is very high and they provide sufficient output.

Disadvantage:

- * Linear POT is required a large force to move their sliding contacts (wipers)
- * ~~The other problems are~~ generate noise
↳ can be contaminated
- * It will create or generate noise during the operation

Strain Gauges -:

- * If a metal conductor is stretched or compressed, its resistance changes on account of the fact that both length & diameter of conductor change.
- * Thus resistivity of the conductor will also ^{be} change.
- * This property of the conductor is called as Piezoresistive effect & the resistance strain gauges are also known as piezoresistive gauges.
- * This device is used for measurement of stress and strain.

*
$$\text{Stress} = \frac{\text{Force}}{\text{Cross Section Area}}$$

$$\sigma = \frac{F}{A}$$

Bowdon tubes, Bell Gauge.

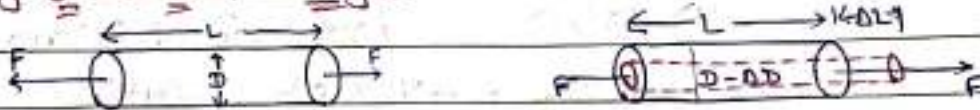
* Strain = $\frac{\text{Extension (change in length)}}{\text{original length}}$

$$\epsilon = \frac{\Delta L}{L}$$

* $\boxed{Y = \frac{\sigma}{\epsilon}}$ $Y = \text{Young's Modulus}$

* Gauge factor = $G_f = \frac{\text{change in resistance}}{\text{strain}} = \frac{\Delta R/R}{\Delta L/L}$

Theory of strain Gauges



* If we apply force to a elastic material, the longitudinal dimension will be increase & lateral dimension will be decrease. (length = increase, area of cross section = decrease)

- * Here $L = \text{length}$ $\Delta L = \text{change in length}$
- $A = \text{Area}$ $\Delta A = \text{change in Area}$
- $D = \text{Diameter}$ $\Delta D = \text{Change in Diameter}$
- $R = \text{Resistance}$ $\Delta R = \text{Change in Resistance}$

* we know $\boxed{R = \rho \frac{L}{A}}$ (i) (find $\Delta R/R$)

TO FIND ΔR , differentiate the above eqⁿ with respect to stress 's'.

$$\frac{dR}{ds} = \frac{1}{A} \frac{\partial L}{\partial s} - \frac{1}{A^2} L \frac{\partial A}{\partial s} + \frac{L}{A} \frac{\partial \rho}{\partial s} \quad \text{--- (ii)}$$

$(A' = -1A^{-2})$

Dividing $R = \rho L/A$ on both side

$$\frac{1}{R} \frac{dR}{ds} = \frac{1}{L} \frac{\partial L}{\partial s} - \frac{1}{A} \frac{\partial A}{\partial s} + \frac{1}{\rho} \frac{\partial \rho}{\partial s} \quad \text{--- (iii)}$$

we know Area^(A) = πr^2 ($D = 2r \Rightarrow r = \frac{D}{2}$)

$$= \pi \left(\frac{D}{2}\right)^2 = \frac{\pi}{4} D^2$$

$$\frac{\partial A}{\partial s} = 2 \cdot \frac{\pi}{4} \cdot D \cdot \frac{\partial D}{\partial s} \quad \text{--- (iv)}$$



Divide area $A = \frac{\pi D^2}{4}$ in eqn (v)

$$\Rightarrow \frac{1}{A} \frac{\partial A}{\partial S} = \frac{(2\pi D) \cdot \frac{\partial D}{\partial S}}{(\pi/4) D^2} = \frac{2}{D} \cdot \frac{\partial D}{\partial S} \quad \text{--- (vi)}$$

Put the value of eqn (v) in eqn (iii)

$$\frac{1}{R} \frac{dR}{dS} = \frac{1}{L} \frac{\partial L}{\partial S} + \frac{2}{D} \frac{\partial D}{\partial S} + \frac{1}{s} \frac{\partial s}{\partial S} \quad \text{--- (vii)}$$

Now, Poisson's ratio = $\frac{\text{lateral strain}}{\text{longitudinal strain}} = \frac{-\partial D/D}{\partial L/L}$

(v) or (vi) longitudinal strain ↑ $\partial L/L$

$$\Rightarrow \partial D/D = -\nu \times \frac{\partial L}{L} \quad \text{--- (viii)}$$

diameter's
reduction

Put the value of eqn (viii) in eqn (vii)

$$\frac{1}{R} \frac{dR}{dS} = \frac{1}{L} \frac{\partial L}{\partial S} + \frac{2\nu}{L} \frac{\partial L}{\partial S} + \frac{1}{s} \frac{\partial s}{\partial S} \quad \text{--- (viii)}$$

for small variations, $\frac{\partial R}{\partial S} = \frac{\Delta R}{\Delta S}$, $\frac{\partial L}{\partial S} = \frac{\Delta L}{\Delta S}$, $\frac{\partial s}{\partial S} = \frac{\Delta s}{\Delta S}$

$$\text{then } \frac{\Delta R}{R} = \frac{\Delta L}{L} + 2\nu \frac{\Delta L}{L} + \frac{\Delta s}{s} \quad \text{--- (ix)}$$

$$\text{we know } G_f = \frac{\Delta R/R}{\Delta L/L} = \frac{\frac{\Delta L}{L} + 2\nu \frac{\Delta L}{L} + \frac{\Delta s}{s}}{\Delta L/L}$$

$$\text{then } \frac{\Delta R}{R} = G_f \cdot \frac{\Delta L}{L} = 1 + 2\nu + \frac{\Delta s/s}{\Delta L/L} \rightarrow \epsilon$$

$$\Rightarrow \frac{\Delta R}{R} = G_f \times \epsilon = 1 + 2\nu + \frac{\Delta s/s}{\epsilon}$$

Resistance change
due to change of
length

Resistance
Change
due to change
of Area

Resistance
Change due
to change
in
Pier's
relative factor

* If we neglected the resistivity of the material.

$$\text{then } \boxed{G_f = 1 + 2\nu}$$

Q) A resistance wire strain gauge with a soft iron wire of small diameter. The gauge factor is 4.2, neglecting the piezo-resistive effect, calculate the poisson's ratio.

$$G_f = 1 + 2\nu + \frac{\Delta R/R}{\epsilon}$$

If piezoresistive effect is neglected,

$$G_f = 1 + 2\nu$$

$$\Rightarrow \nu = \frac{G_f - 1}{2} = \frac{4.2 - 1}{2} = 1.6 \text{ (Ans)}$$

Unbonded Metal Strain Gauges:-

* In this figure a wire stretched betⁿ two points in an insulating medium such as air.

* The wires is made of copper nickel alloys or nickel iron alloys.

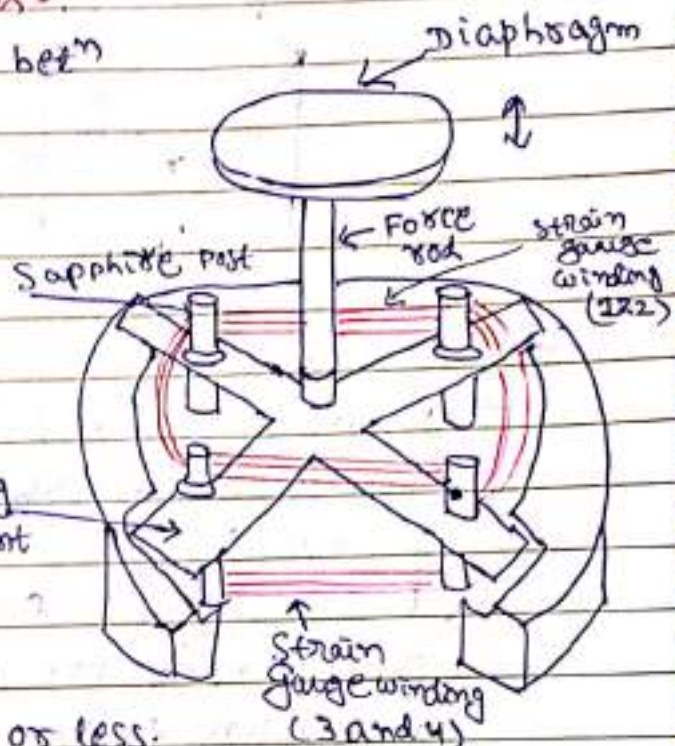
~~Observation~~

* Diameter of the wire is 0.003 mm.

* Gauge factor (G_f) = 2 to 4

* Force = 2 mN

* length of the wire = 25 mm or less.



* Here a spring element is connected via a rod to a diaphragm which is used for sensing of pressure.

* The unbonded metal wire gauges used for transducer applications, employ preload resistance wires connected in a wheatstone bridge.

* At initial preload, the strains and resistance of the four arms are equal and output voltage $e_o = 0$.

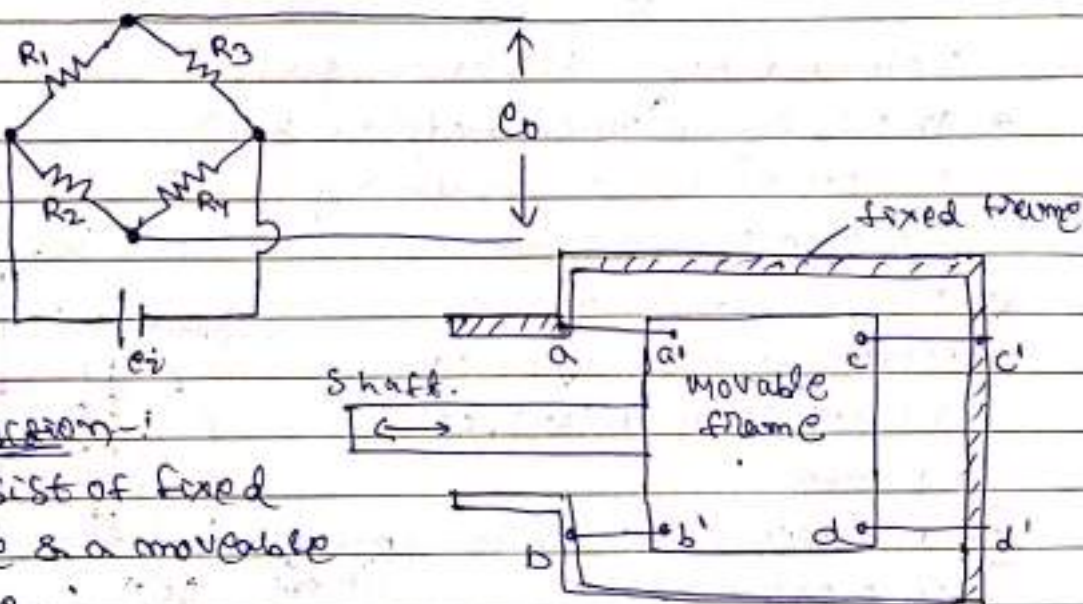
* Application of pressure produces a small displacement which is about 0.004 mm (full scale).

* The displacement increase tension in two wires

and decrease it in the other two, thereby increase the resistance of two wires which are in tension and decreases it in the other two of the remaining two wires.

Due to

* This unbalance of resistance, we can get output voltage. ~~Electric~~ resistance of each arm is 120Ω to 1000Ω , the i/p voltage to the bridge is 5 to 10V. and the output of the bridge is 20mV to 50mV.



Construction:-

* It consists of fixed frame & a movable frame.

* The movable frame connected on a shaft which move under the application of force or strain which has to be measure.

* The 4 strain gauge wire having uniform cross section area and equal length are connected in such a manner that one end is connected to the fixed frame & other end is connected to the movable frame.

* The resistance of the wire are equal in magnitude.

* This device is used for measure ^{ment of} force, stress or displacement.

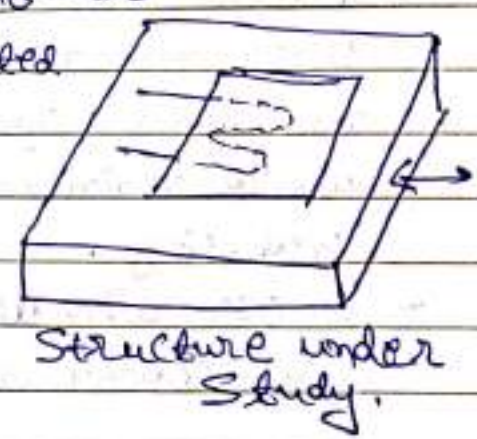
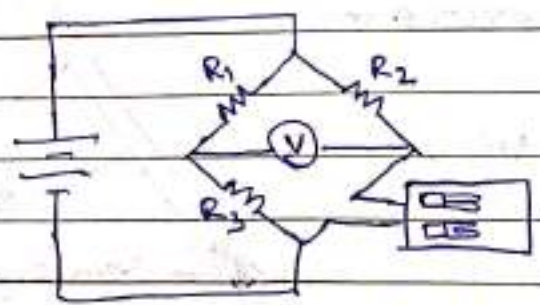
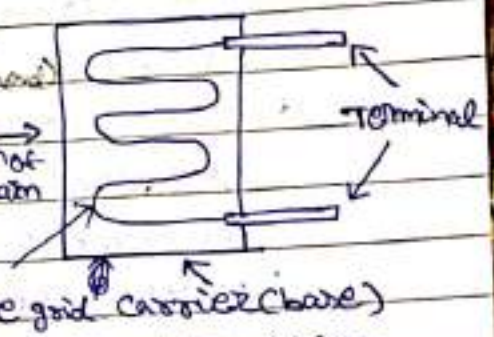
* Here the 4 strain gauge wire form a Wheatstone bridge circuit.

Ques

- * If F is zero, then resistance of each strain gauge wire is equal in magnitude & we can't get the output voltage ($e_o = 0$)
- * when we applied the force on the shaft the moving frame is move & it will change the resistance of the strain gauge wire. Due to change in resistance we can find the output.

Bonded wire Strain Gauges:-

- * The bonded metal-wire strain gauges are used for both stress analysis and for construction of transducers.
- * It consists of a thin sheet insulating material such as paper, bakelite, ^{some type of plastic} ~~composites~~ ^{RESISTIVE layer}
- * Here, we consider a strain gauge wire of uniform cross sectional area and its diameter is about 0.025mm or less.
- * This wire is uniformly semented bet^{ween} two thin insulating material ^{which} ~~so~~ prevent it from any mechanical damage.
- * The spreading of wire permits a uniform distribution of stresses over the grid.
- * Here, two terminal are taken out from the wire and consider as terminal lead.
- * This strain gauge material is bounded with an additional material for study purpose. ~~at the end~~
- * Here, the strain gauge is connected to a wheatstone bridge.



- * If we don't apply stress to the wire, then the

output will be zero. But if we apply stresses on the strain gauge, then the value of resistance in the wheatstone ^{bridge} will be unequal & we can get the output.

* The resistance wire strain gauges should have the following characteristics.

a) The strain gauge should have a high value of gauge factor (G_f)

b) The resistance of the strain gauge should be as high as possible to minimize the effects of undesirable variations of resistance in the measurement circuit.

c) The strain gauge should not have any hysteresis effects in its response.

d) The strain gauges should have a low resistance temperature co-efficient. This is essential to minimize errors on account of temp. variations which affect the accuracy of measurements.

Resistance Thermometer :-

* The resistance of a conductor changes when its temp. is changed. This property is utilized for measurements of temperature.

* The variation of resistance (R) with temp. $T(^{\circ}K)$ can be represented by $R = R_0(1 + d_1T + d_2T^2 + \dots + d_nT^n)$

where R_0 = resistance at temperature $T=0$ &

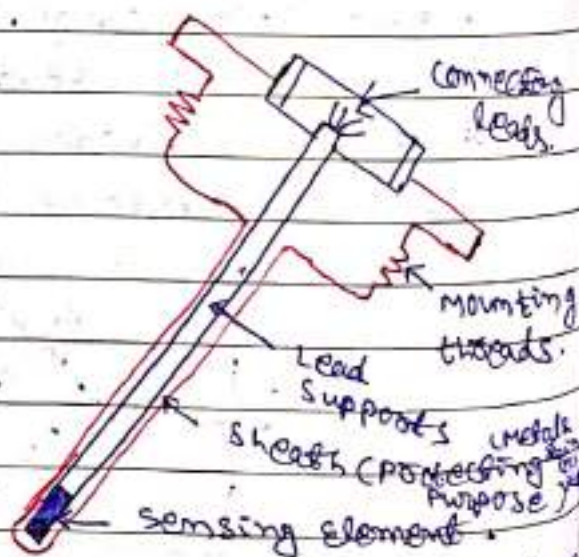
$d_1, d_2, d_3, \dots, d_n$ are constants.

* platinum is used in this

thermometer as it can withstand high temperatures

while maintaining excellent stability.

* we can also use nickel and copper also.

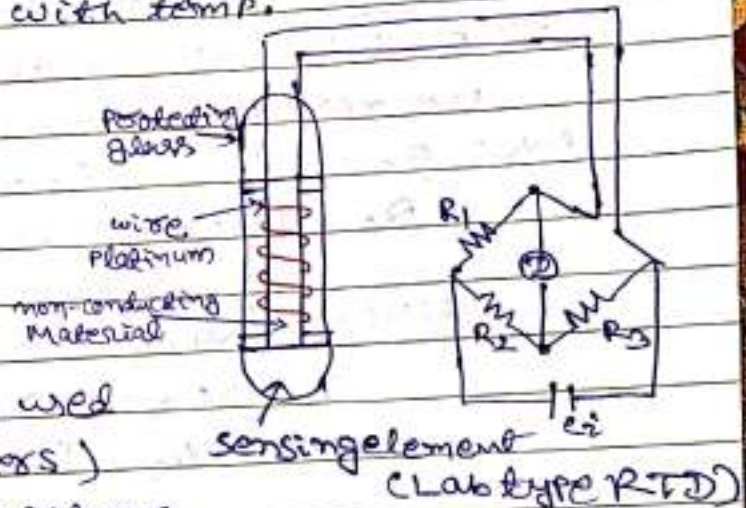
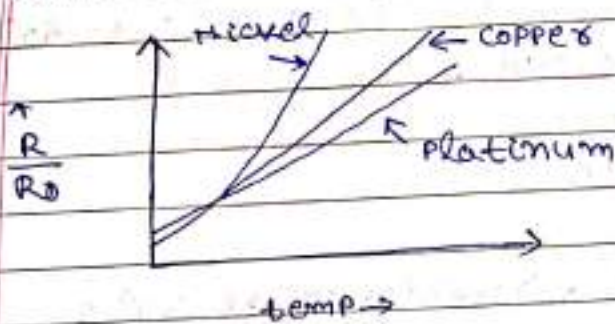


Industrial platinum resistance thermometer

	Min	Max
* Platinum	-260°C	110
* COPPER	0°C	180
* NICKEL	-220°C	300

* Requirements of a conductor material to be used in RTD are -:

- a) The change in resistance of material per unit change in temp. should be as large as possible (error minimized)
- b) The material should have a high value of resistivity so that minimum volume of material is used for the construction of RTD.
- c) The resistance of materials should have a continuous and stable relationship with temp.



(Characteristics of Materials used for resistance thermometers)

Sensing element (Lab type RTD)

* Supply electric supply to wheatstone bridge ckt.

* Set the ~~resistance~~^{deflector} value to a null position (zero) by adjusting the resistance value.

* Then set the instrument according where we can measure the temp.

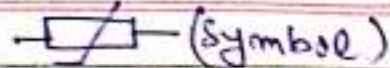
* The sensing element sense the temp.

* When temp rises, the length of the ~~drag~~ wire increases & when temp decreases, the length of the wire decreases,

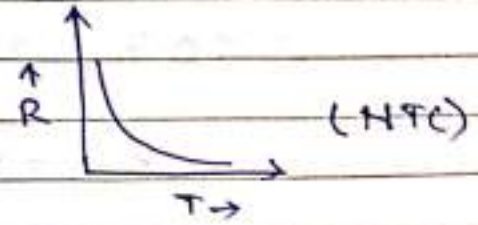
$$R = \frac{\rho L}{A}$$

& we can get the resistance value by the help of deflector.

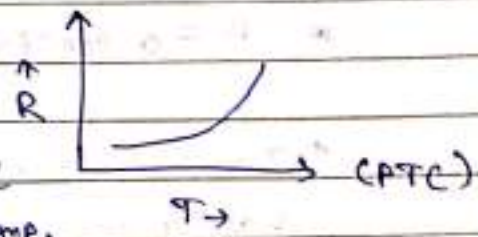
Thermistors



- * It is a semiconductor device whose resistance depends on temperature.
- * It is also known as temperature sensitive resistance.
- * It is of two type.
 - a) NTC (Negative temp. coefficient)



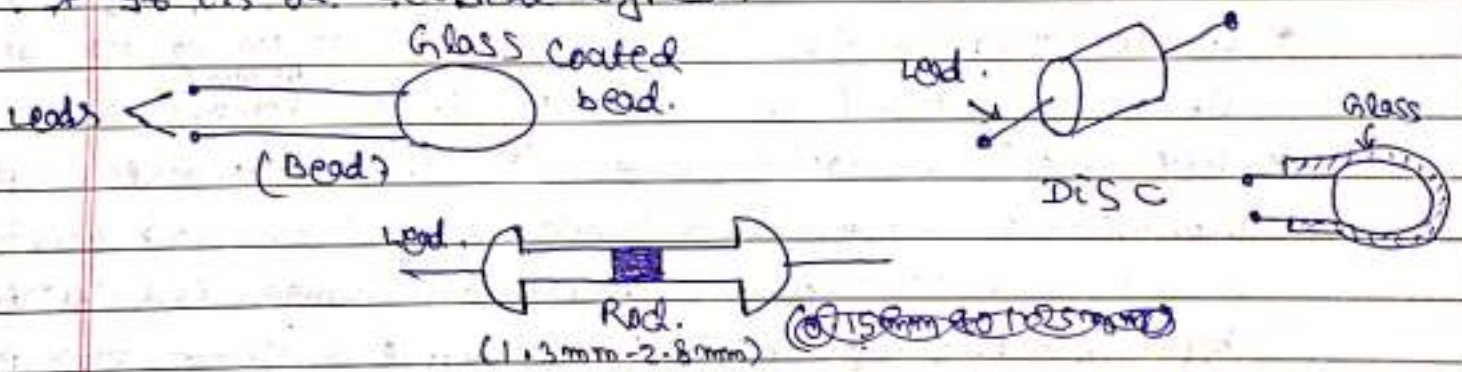
- * Here resistance is ~~decrease~~ decrease with increase in temp.
- b) PTC (Positive temp. coefficient)



- * Here resistance is increase with increase in temp.
- * It more efficient than RTD because it measure very small change in temp.
- * Measurement range of thermistor = -60°C to 15°C
- * Resistance of thermistor = 0.5Ω to $0.75\text{M}\Omega$

Construction

- * Thermistors are composed of a mixture of metallic oxides such as nickel, cobalt, copper, iron etc.
- * It is of several types.



- * A thermistor in the form of a bead is smallest in size & the bead may have a diameter of 0.015mm to 1.25mm .
- * Beads may be sealed in the tips of solid glass rods to form probes. Glass probes have a diameter of 2.5mm & length is 6mm to 50mm .
- * Discs are made by pressing material under high pressure into cylindrical flat shapes with diameters 2.5mm to 25mm .

$$^{\circ}\text{C to K} = 273.15$$

Resistance-Temperature Characteristics of Thermistors:

- * Mathematical expression for the relationship betⁿ the resistance of a thermistor and absolute temp. of thermistor is

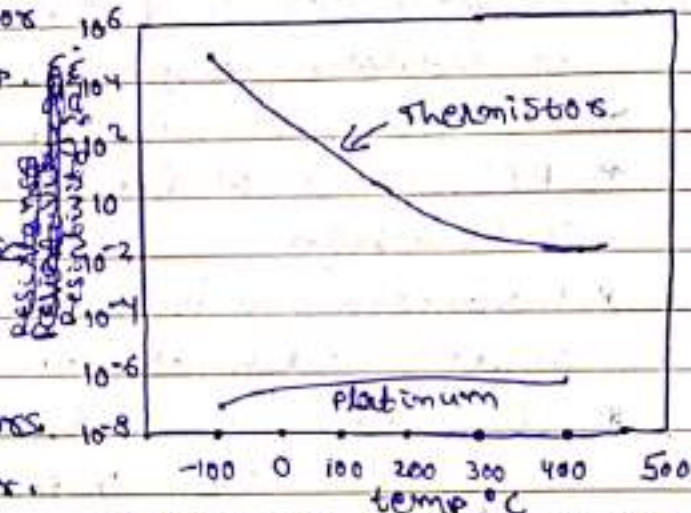
$$R_{T_1} = R_{T_2} \exp \left[\beta \left(\frac{1}{T_1} - \frac{1}{T_2} \right) \right]$$

where R_{T_1} = resistance of the thermistor at absolute temp. T_1 ; $^{\circ}\text{K}$

R_{T_2} = resistance of the thermistor at absolute temp. T_2 ; $^{\circ}\text{K}$

- * β = a constant depending upon the material of thermistor, typically 3500 to 4500 $^{\circ}\text{K}$.

- * In this graph, a thermistor has a very high -ve temp. co-efficient



- * Here, we can see the resistance temp. characteristics of platinum which is commonly used material for resistance thermistors.

- * Let us compare the char. of two materials.

- * Betⁿ -100°C to 400°C , the thermistor changes its resistivity from 10^5 to $10^{-2} \Omega\text{m}$, a factor of 10^{-7} while platinum changes its resistivity by a factor of about 10 within the same temp. range.

- * This explains the high sensitivity of thermistors for measurement of temp.

- * For a limited range of temp. (in case of linear approximation) will be

$$R_{\theta} = R_{\theta_0} [1 + \alpha_{\theta_0} \Delta \theta]$$

* A thermistor curve can be represented as Steinhart-Hart eqn $\frac{1}{T} = A + B \log_e R + C (\log_e R)^3$

T = temperature; $^{\circ}K$

R = resistance of thermistor; Ω

A, B, C = curve fitting constants (3 data points on the curve)

* If the data points are chosen in between $100^{\circ}C$

then a simpler eqn is $T = \frac{B}{\log_e R - A} - C$

* Another eqn used for resistance-temp. curve of thermistors is $R_T = R_0 \exp(b/T)$

R_T, R_0 = resistance of thermistor at temp $T^{\circ}K$ and ice point respectively.

Linear Variable Differential Transformer (LVDT)

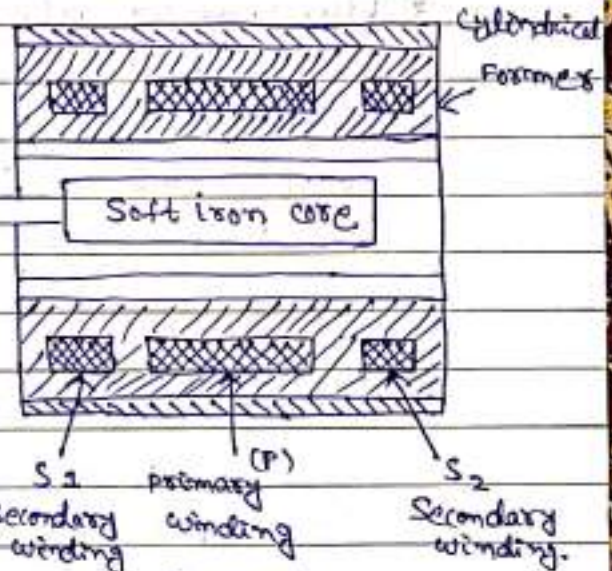
* Most widely used inductive transducer is LVDT.

* The T/F consists of a single

primary winding (P) & two

secondary windings S_1 & S_2

wound on a cylindrical
former.



* The secondary windings have equal no. of turns and are identically placed on either side of the primary winding.

* The primary winding is connected to an AC source.

* A movable soft iron core is placed inside the former.

* The displacement to be measured is applied to the arm attached to the soft iron core.

* The core is made of ~~high~~ nickel, iron which is hydrogen annealed & its permeability is high.

heat treatment
to eliminate hydrogen.

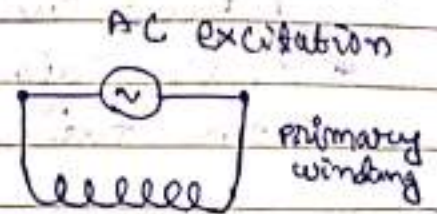
ability of metal to generate
magnetic flux.

* This gives low harmonics, low null voltage and a high sensitivity & reduce eddy current loss.

a current induced in the conductor by a varying magnetic field.

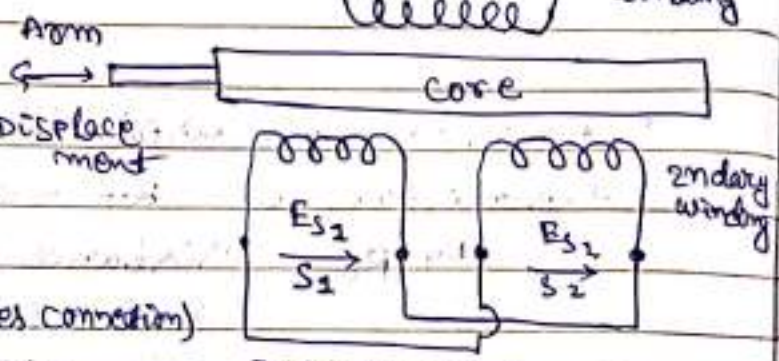
* The freq. of A.C applied to primary windings may be bet'n 50Hz to 20kHz.

* 1^o winding current → Magnetic field (flux) created → EMF induced → Mutual inductance to 2^o winding.



* O/P Vtg. in

Secondary winding S_2 is displaced. E_{S1} & S_2 is E_{S2}



* then Diff. O/P Vtg.

$$E_o = E_{S1} - E_{S2} \text{ (Series connection)}$$

* when the core is at its normal position (null) position.

* Flux linking with both 2^o windings is equal.

$$\text{So, } E_{S1} - E_{S2} = 0$$

* Core left side of null position

more flux in S_1 & less flux in S_2 .

So output Vtg. $E_{S1} > E_{S2}$. So $E_o = E_{S1} - E_{S2}$ (+ve value)

(O/P Vtg. is in phase with Primary Vtg.)

* Core Right side of null position.

More flux in S_2 & less flux in S_1 .

So output Vtg. $E_{S2} > E_{S1}$. So $E_o = E_{S1} - E_{S2}$ (-ve value)

(O/P Vtg. is 180° out of phase with 1^o Vtg.)

* Voltage change in 2^o winding & movement of core.

* By calculate the o/p Vtg. increasing or decreasing we can determine the direction of motion.

Capacitive Transducers -

* The principle of operation of capacitive transducers is based upon the eqn $C = \epsilon A/d$

$$C = \epsilon_0 \epsilon_r A/d$$

A = overlapping area of plates; m^2

d = distance betⁿ 2 plates; m

$\epsilon = \epsilon_0 \epsilon_r$ = permittivity of medium; F/m

ϵ_r = relative permittivity

ϵ_0 = Permittivity of free space; $(8.85 \times 10^{-12} \text{ F/m})$

* The capacitive transducer works on the principle of change of capacitance which may be caused by

a) Change in overlapping area (A)

b) Change in the distance (d) betⁿ the plates.

c) Change in dielectric constant. ($\epsilon_r = \frac{\epsilon}{\epsilon_0}$)

* The capacitance may be measured with bridge circuit.

The output impedance of a capacitive transducer is

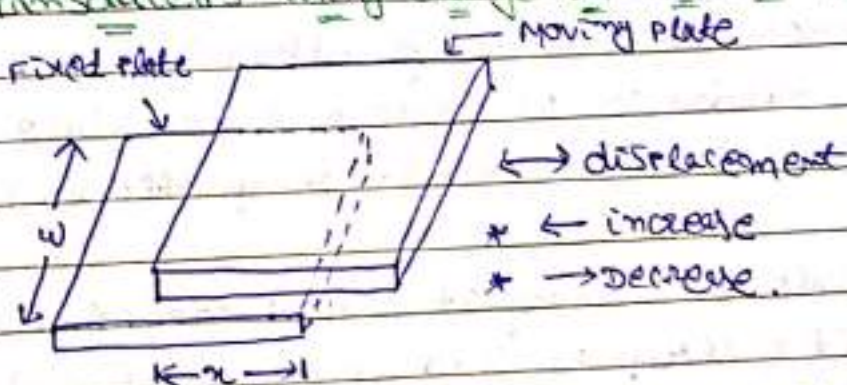
$$X_c = \frac{1}{2\pi f C}$$

f = freq.

C = capacitance.

* Generally, the o/p impedance of a capacitive transducer is high.

Transducers using change in Area of plates -



* For a parallel plate capacitor, the capacitance is

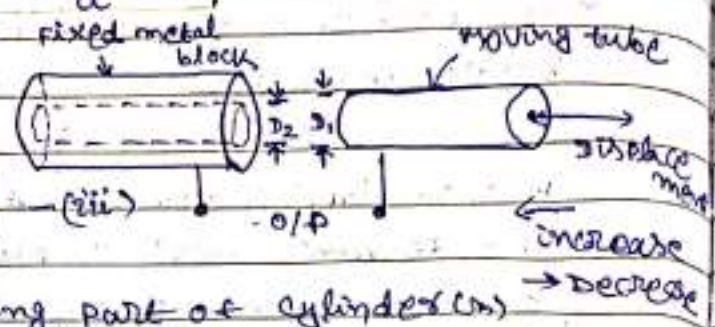
$$C = \frac{\epsilon A}{d} = \frac{\epsilon x w}{d} \text{ F} \quad - (1)$$

x = length of overlapping part of plates, m.
 w = width of overlapping part of plates, m.

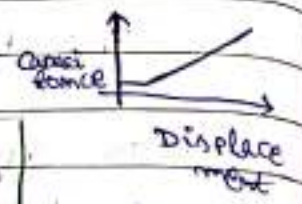
Sensitivity (S) = $\frac{dC}{dx} = \epsilon \frac{w}{d} F/m$ (ii)

* For a cylindrical capacitor, the capacitance is

$C = \frac{2\pi\epsilon m}{\log_e(D_2/D_1)} F$ (iii)



- m = length of overlapping part of cylinder (m)
- D₁ = inner diameter of cylinder (m)
- D₂ = outer diameter of cylinder (m)



Sensitivity (S) = $\frac{dC}{dx} = \frac{2\pi\epsilon}{\log_e(D_2/D_1)} F/m$

Advantages of capacitive transducers:

- a) They required very small forces to operate them & hence are very useful for use in small systems.
- b) They are extremely sensitive.
- c) They have a good frequency response (up to 50 kHz)
- d) They have a high input impedance, effective resistance

Disadvantages:

- a) The metallic parts of the capacitive transducers must be insulated from each other & frames must be earthed.
- b) The capacitive transducers show non-linear behaviour in few times (due to edge effect)
- c) The o/p impedance of capacitive transducers show high impedance (due to loading effects)

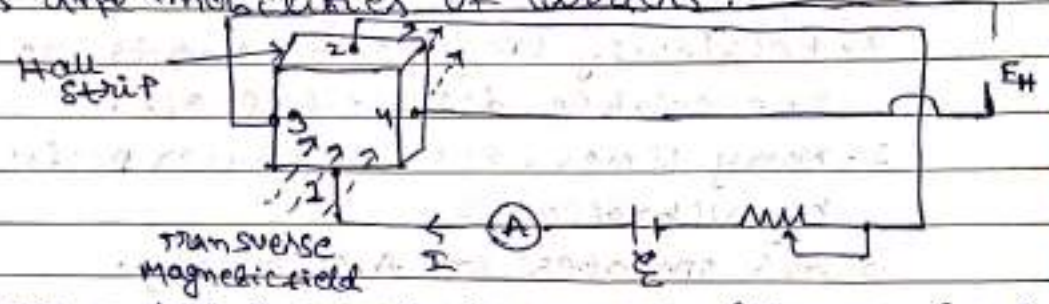
50) Hall effect transducers:

* The principle of working of a Hall effect transducer is that if a strip of conducting material carries a current in the presence of a transverse magnetic field, a potential difference is produced between the opposite edges of the conductor.

* Transverse mag. field: perpendicular magnetic field measured in a plane perpendicular to the direction of current flow.

* Here the magnitude of the voltage depends upon the current, ^{the} strength of magnetic field and the property of the conductor called Hall effect.

* The hall effect is present in metals and semiconductors in varying amount, depending upon the densities and mobilities of carriers.



* In this fig., the current is passed through lead 1 and 2 of the strip.

* The o/p leads connected to edges 3 & 4 are at the same potential when there is no transverse magnetic field passing through the strip.

* When a transverse magnetic field passes through the strip, an o/p voltage appears across the o/p leads.

* This voltage is proportional to the current and the magnetic field strength.

* The o/p vty. is
$$E_H = K_H I B / t$$

K_H = Hall effect coefficient ; $\left(\frac{V \cdot m}{A \cdot Wb \cdot m^{-2}} \right)$

t = thickness of strip ; (m)

I = current (A) , B = flux density Wb/m^2

* The Hall effect emf is very small in conductors & is difficult to measure. But in case of semiconductors (germanium), the emf can be measured.

Advantages of LVDT

1. High range of measurement of displacement.
2. Low power consumption.
3. Low hysteresis loss.
4. High input & high sensitive.

Disadvantages of LVDT

1. Relatively large displacements are required for appreciable differential o/p.
2. Many times, the transducer performance is affected by vibrations.
3. It's operates in A.C Supply.
4. Temp. affects the performance of the transducer.

CHAPTER - 08

CRO - (Cathode Ray Oscilloscope) → Graphically display signal

* Cathode Ray Oscilloscope is an electronic device which displays & measures the signals by its shape, frequency & phase shift.

* It is constructed by its several circuit.

CRT - (Cathode ray tube)

* It is the heart of the CRO. It is a vacuum tube of special geometrical shape and converts an electrical signal into visual one.

* Here an electron gun is there, which generated electron beam.

* First it deflected by two pairs of deflection plate, then strike on fluorescent screen & produces visible light.

* It has two main parts

a) Electron gun Assembly b) Deflection System
(Vertical & Horizontal)

Y-input:-

* It is the main i/p of CRO where i/p signal is connected. The wave forms of input signal displayed on the CRT screen.

Vertical Amplifier:-

* It is a set of pre amplifier which receives the external i/p signal.

* This signal is connected to the vertical deflection plate through a Delay line.

Delay line:-

* It delays the striking of electron beam on the screen & synchronize the arrival of time base generator signal starts sweeping horizontally. It is around 0.25 m. sec.

Trigger Circuit:-

* It takes the sample of i/p signal voltage and feeds to time base generator to start only when i/p 'y' signal is present.

Time base Generator:-

* It produces a saw tooth wave form.

* This wave form is used to sweep the electron beam horizontally on the screen.

* This is controlled by Time/Division knob.

* The saw tooth wave control the horizontal deflection of electron beam along x-axis.

Horizontal Amplifier:-

* It amplifies the saw tooth wave form which is connected to horizontal plate of CRT.

* It helps to move the electron beam from left to right on CRT screen.

HV/LV Power Supply - It provides the necessary high voltages to CRT & low voltage to other circuit of CRO.

